

Weak lensing  
cluster mass

Introduction

What we did

- Sources of noise
- Profile uncertainty
- Optimized apertures
- Mass results

Modelling the  
Covariance

Conclusions

# Minimum variance weak lensing cluster mass estimates

AlfA Lens/Cosmology Seminar

2012-08-28

Daniel Gruen, G. Bernstein, T. Y. Lam, S. Seitz (2011)

# Structure

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# Clusters of Galaxies

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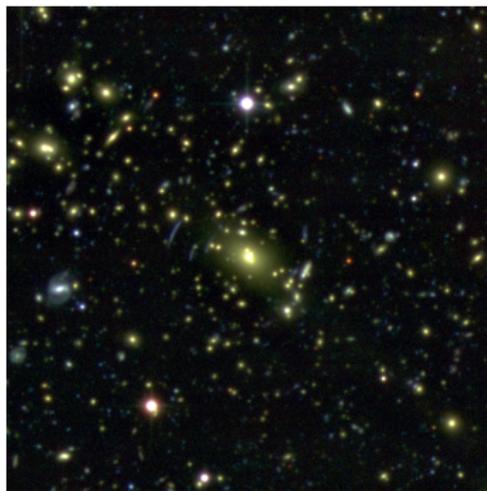
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- most massive structures:  
 $10^{14} M_{\odot}$ , 1Mpc
- dark matter, gas, galaxies
- formation  $\leftrightarrow$  cosmology



RXJ2248, source: WFI / own reduction

# Weak Lensing

Weak lensing  
cluster mass

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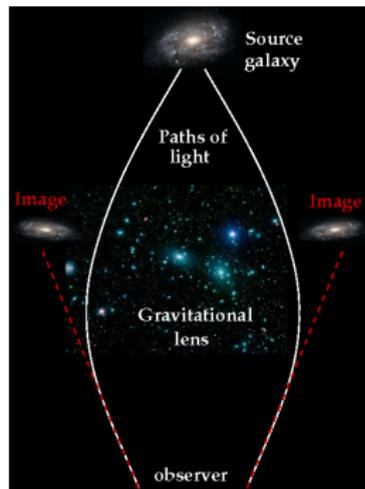
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- Clusters bend space-time and light
- Multiple images: strong lensing
- shear: weak lensing
- mass measurements
- model fitting
- aperture mass



Source: galileospendulum.org

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	$< 0$	$> 0$
$\text{Re}[\gamma]$		
$\text{Im}[\gamma]$		

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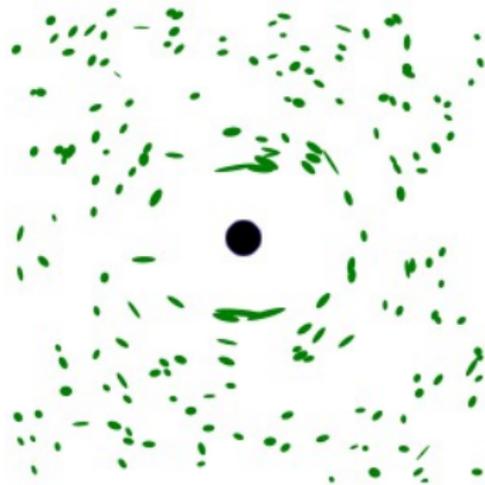
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$$\gamma_t(\theta) = \langle \kappa(\theta') \rangle_{\theta' < \theta} - \kappa(\theta)$$

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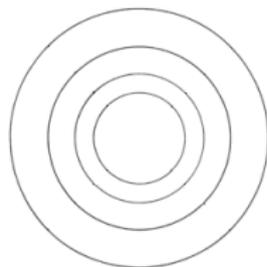
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# Faces of galaxy clusters

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M. Gruendl, Institute of Psychology, Uni Regensburg

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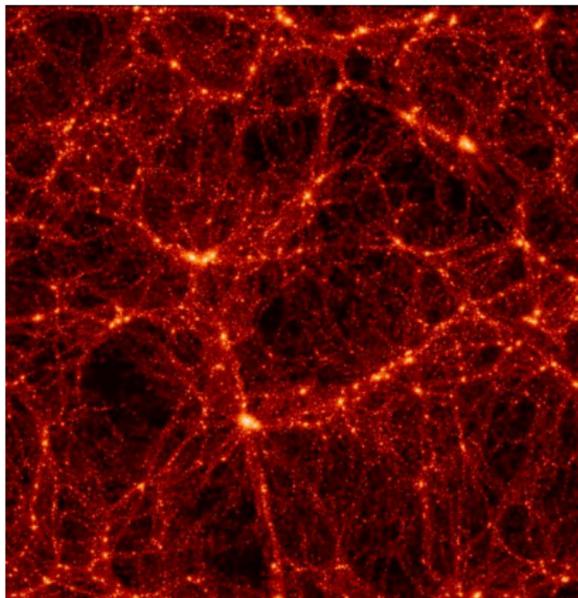
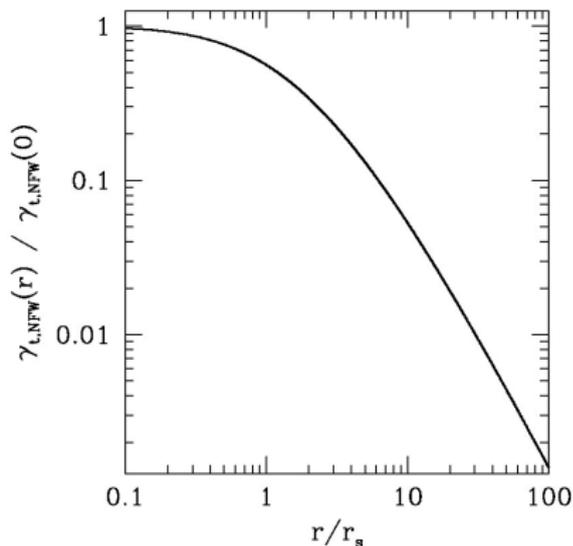
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Simulations: van den Bosch, MPA

# Tall tales of NFW

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Yes,

- average profile of dark matter halos

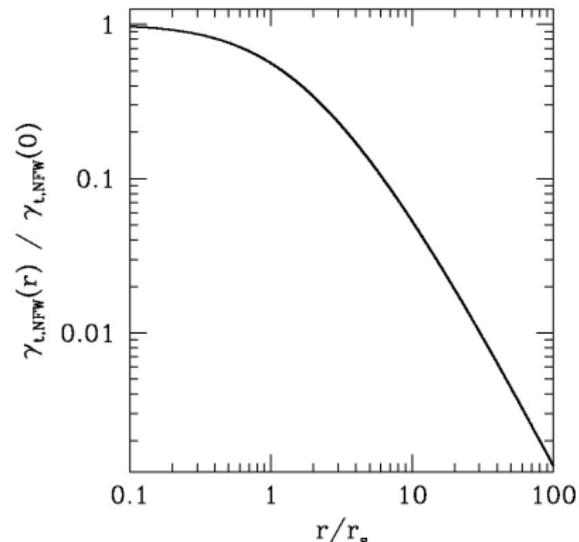
but ...

- asphericity
- concentration scatter
- substructure
- surrounding structures
- core and outskirts

$$\rho(r) = \frac{\rho_0}{(r/r_s)(1+r/r_s)^2}$$

Navarro, Frenk, White (1996)

$$c = r_{200}/r_s = c(M, z)$$



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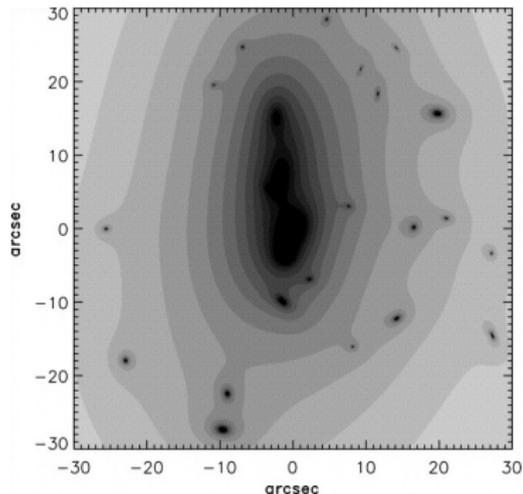
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Source: Verdugo et al. (2007)

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$\sigma_{\log c} \approx 0.18$   
Bullock et al. (2001)

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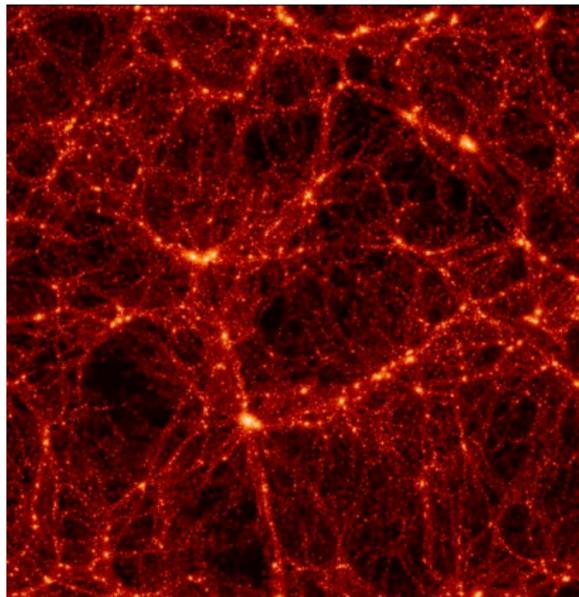
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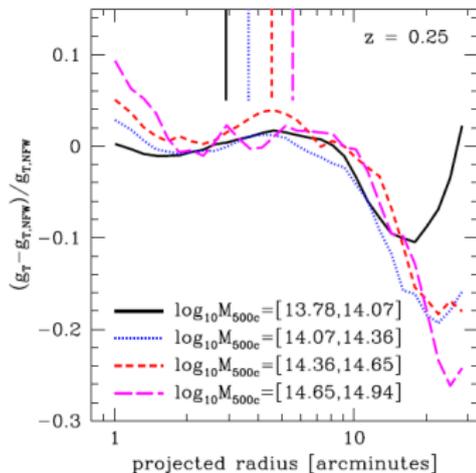
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Source: Becker & Kravtsov (2011)

# What we did: four steps

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## Sources of Noise

NFW signal + shape noise + LSS + intrinsic mess

## Intrinsic profile variability

Can we explain the scatter in shear profiles we see?

## Optimized apertures

What do optimized apertures look like?

## Mass uncertainty

Does it help at all?

# Sources of noise in Weak Lensing

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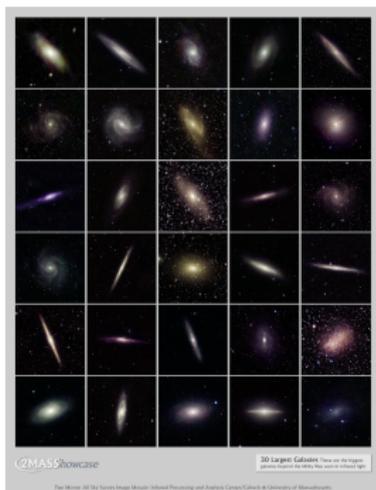
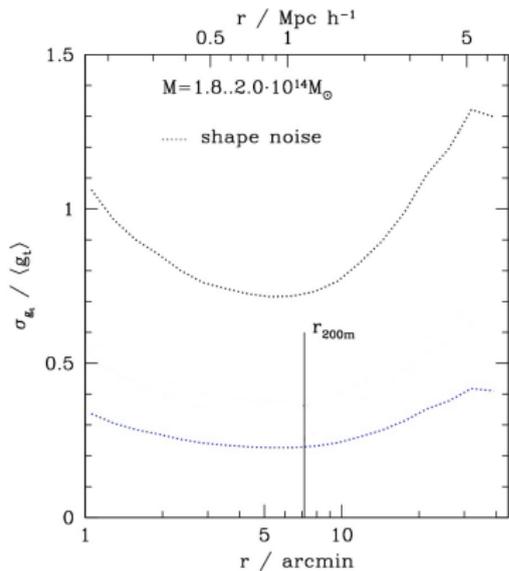
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Source: 2MASS

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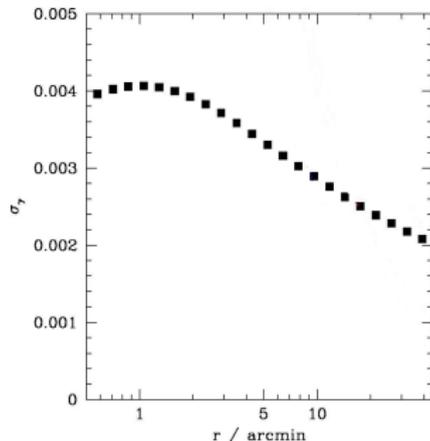
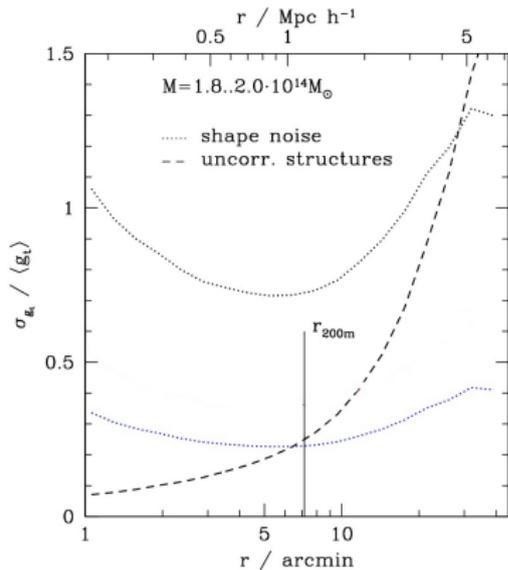
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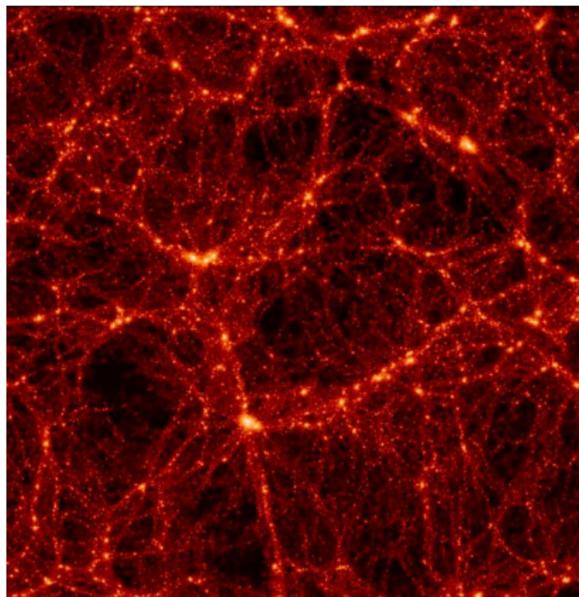
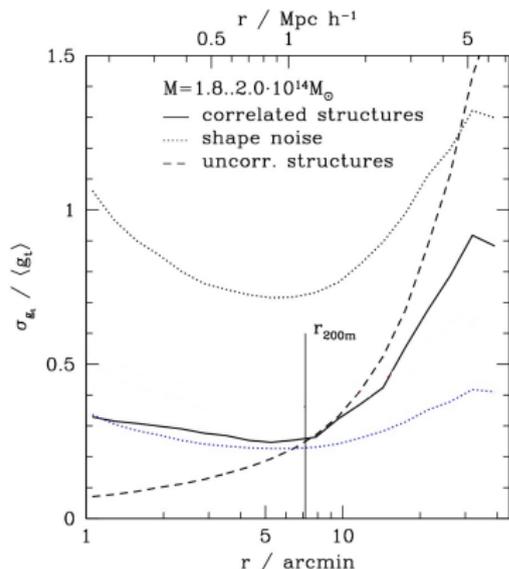
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14,000 clusters  $> 10^{14} M_{\odot}$   
at  $z = 0.245$

# Profile uncertainty: components

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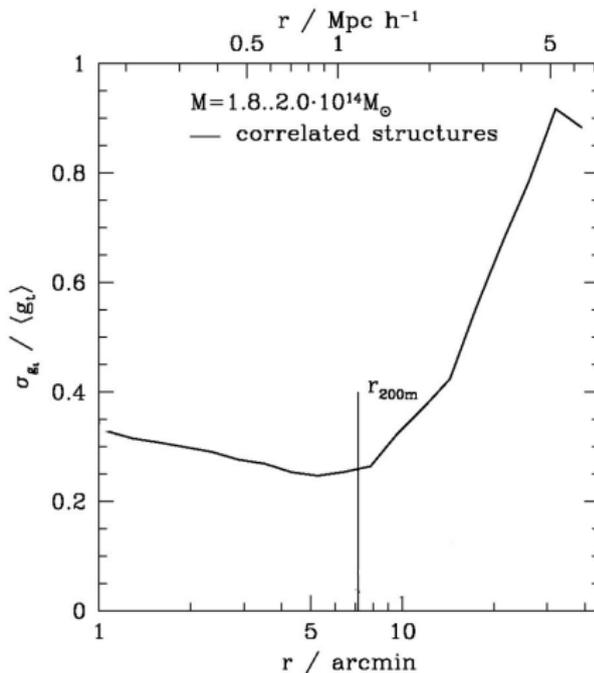
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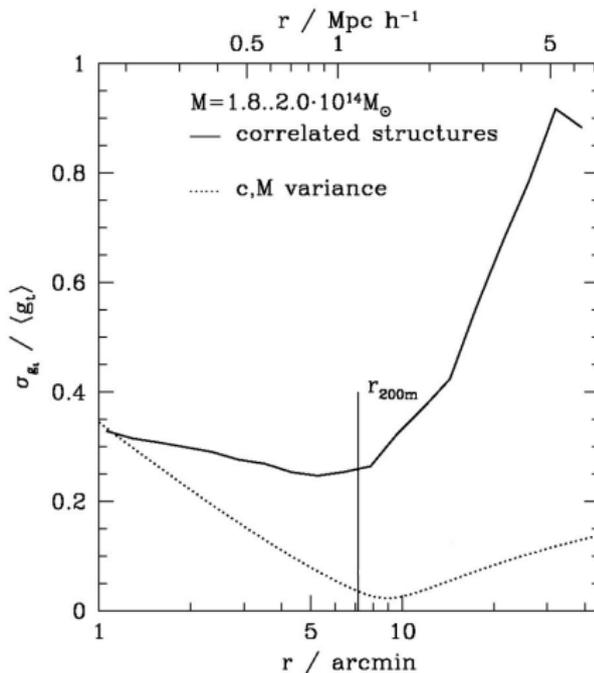
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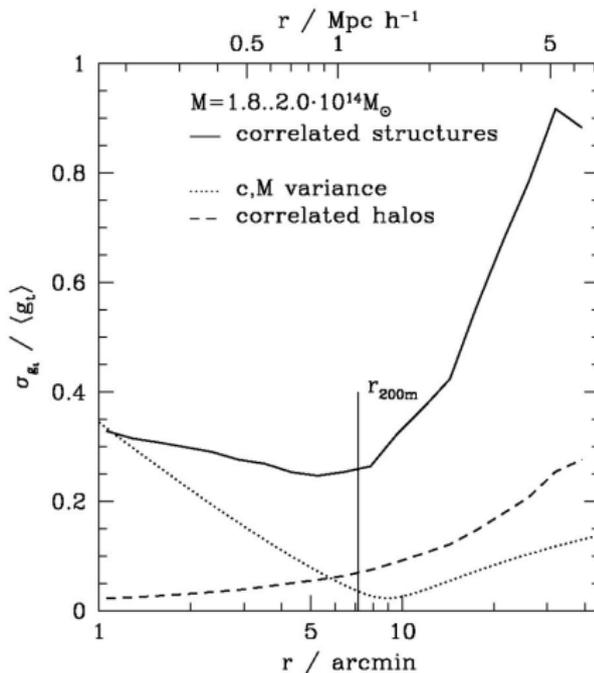
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# Aperture mass

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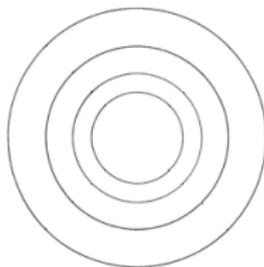
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$$M_{\text{ap}} = \int 2\pi\theta \, d\theta \, u(\theta) \cdot \kappa(\theta)$$
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$$M_{\text{ap}} = \sum_i Q_i \gamma_i$$



Minimum variance aperture

$$\vec{Q} \propto \hat{C}^{-1} \vec{\gamma}_{\text{true}}$$

for uncorrelated LSS: Dodelson (2004), Maturi et al. (2005)  
including correlated structures: this work

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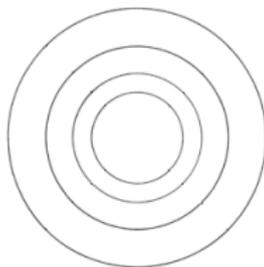
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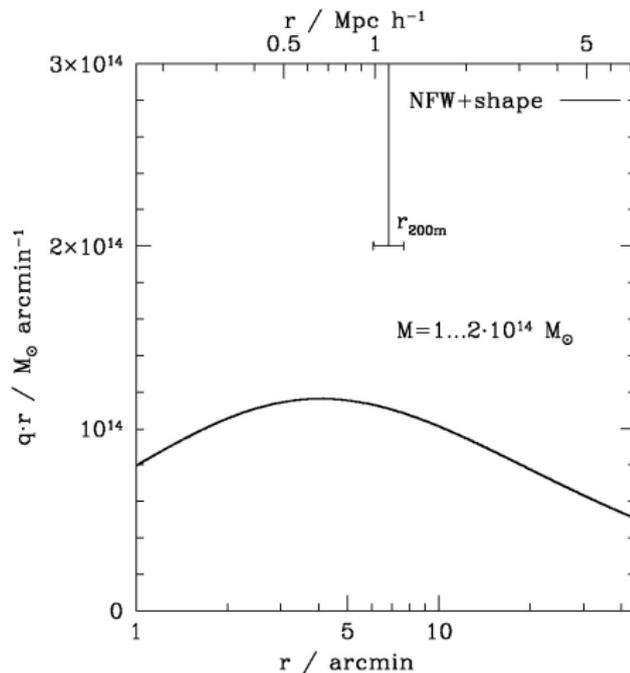
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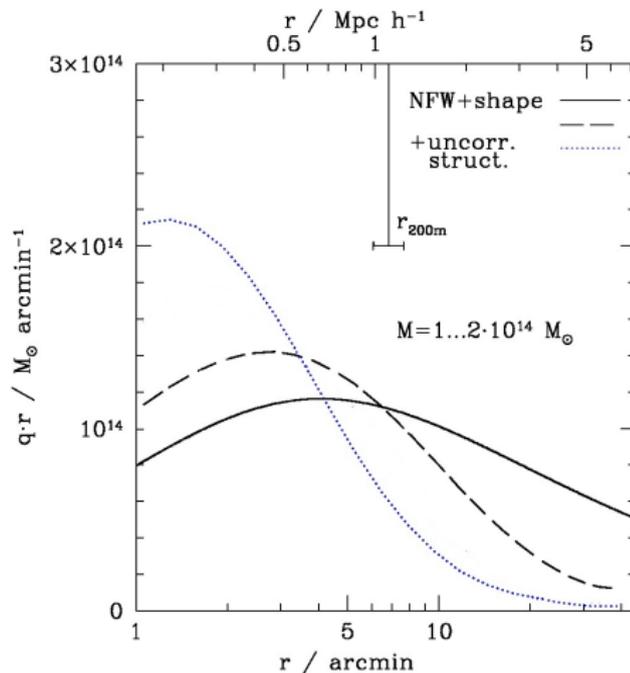
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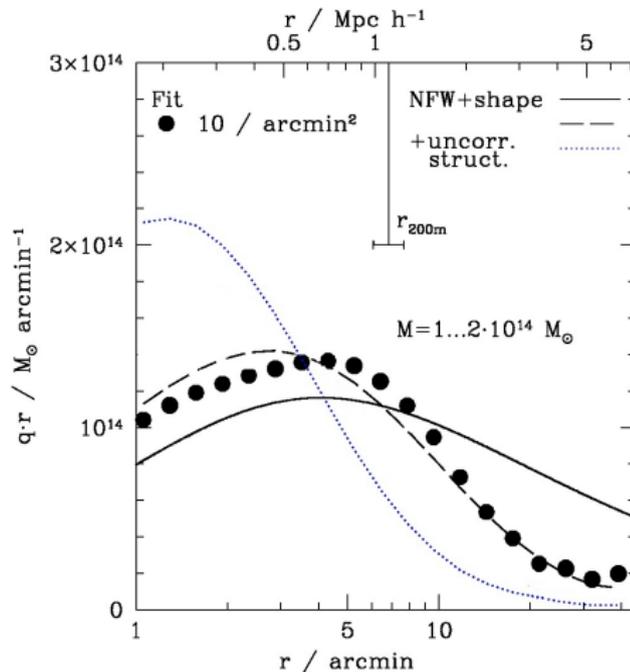
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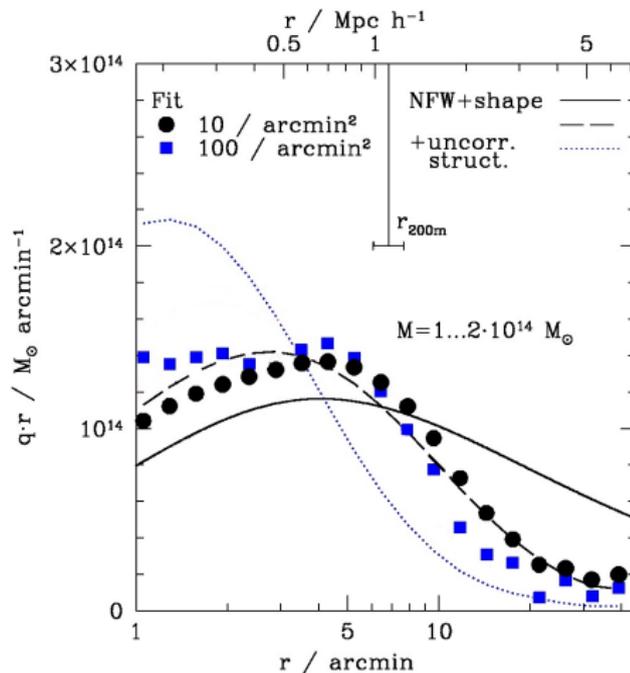
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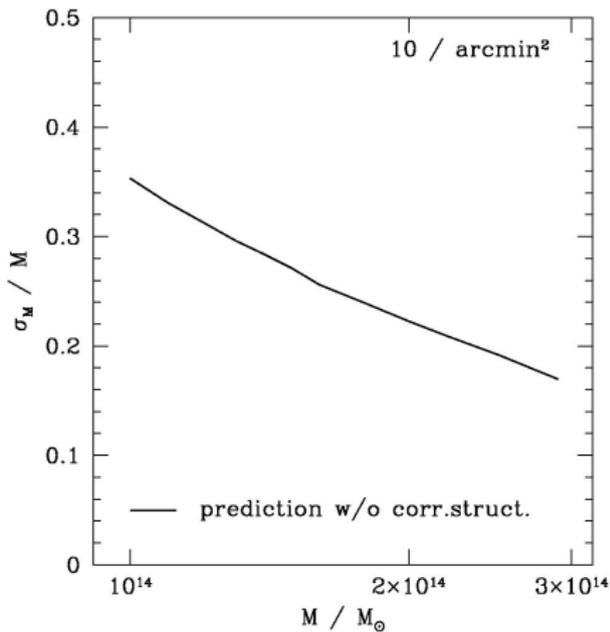
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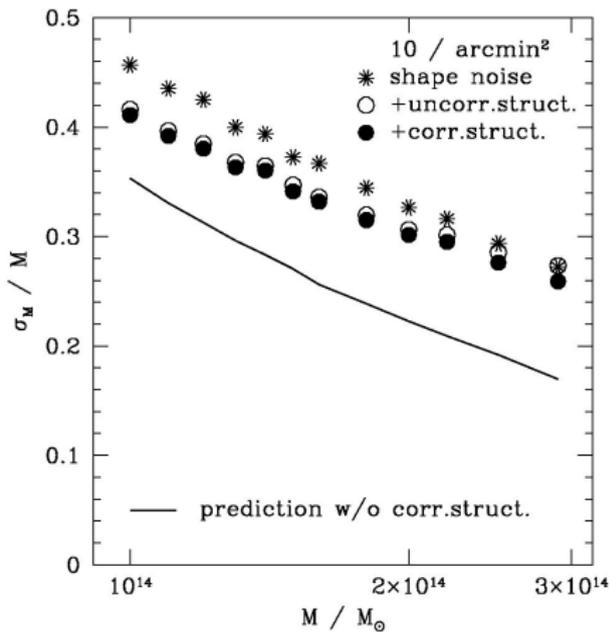
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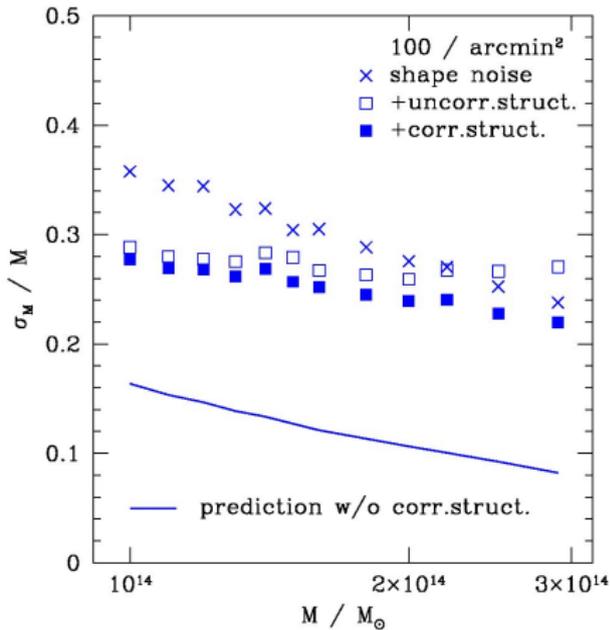
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## Why model the covariance of cluster shear?

- prediction of mass uncertainty
- full Bayesian mass estimation
- peak detection completeness

## Idea

Use two simple components:

- concentration variation
- Poisson noise of correlated halos

and rescale to fit

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# Modelling the Covariance [preliminary]

Weak lensing  
cluster mass

Can we model the variations of cluster shear profiles...  
• in small mass bins using these components?

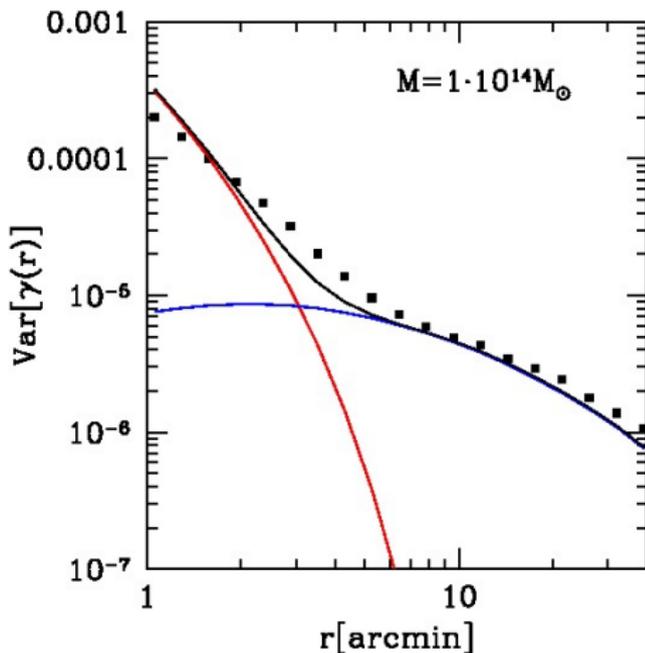
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# Modelling the Covariance [preliminary]

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Can we model the variations of cluster shear profiles...

- over a range of masses?

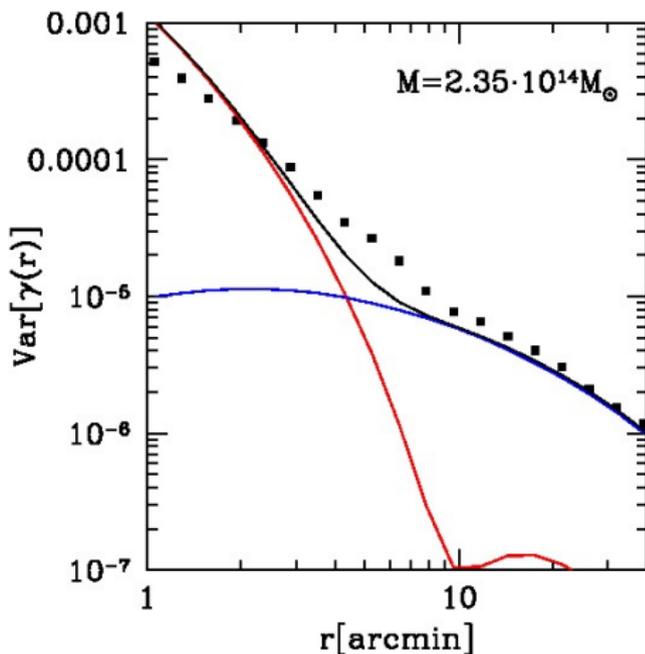
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Can we model the variations of cluster shear profiles...

- also for off-diagonal components?

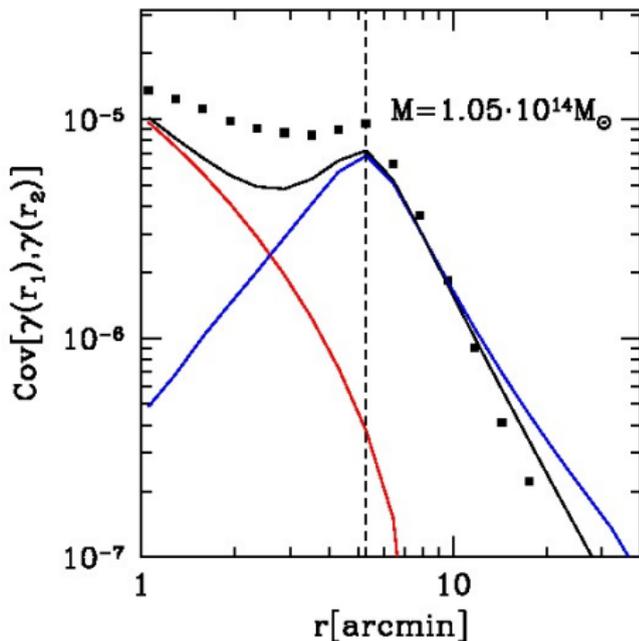
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## NFW

spherical NFW is only a good approximation on *average*

## Halo structure

$(M, c)$  is no sufficient description either  
possible to model variations

## Mass uncertainty

$\sigma_M >$  naive expectations; deeper only marginally better

## Optimized apertures

modest improvements  
doing half sometimes worse than doing nothing

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