



# On the secular evolution of the ratio between gas and dust radii in protoplanetary discs:

TESTING THE EFFICIENCY OF RADIAL DRIFT

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*Collaborators: Giovanni Rosotti, Giuseppe Lodato, Leonardo Testi, Leon Trapman*

*Special thanks: Richard Booth, Marco Tazzari and Alice Somigliana*

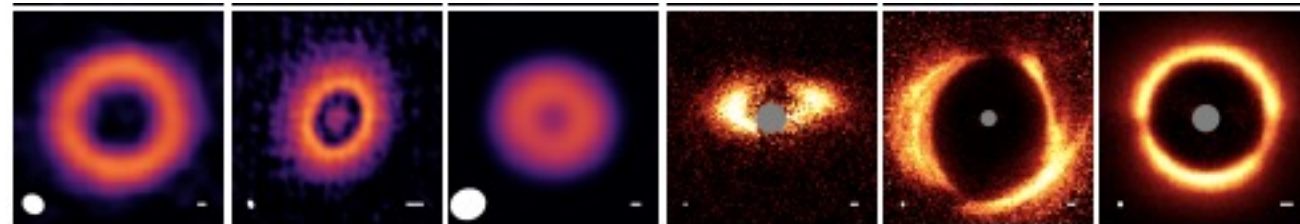
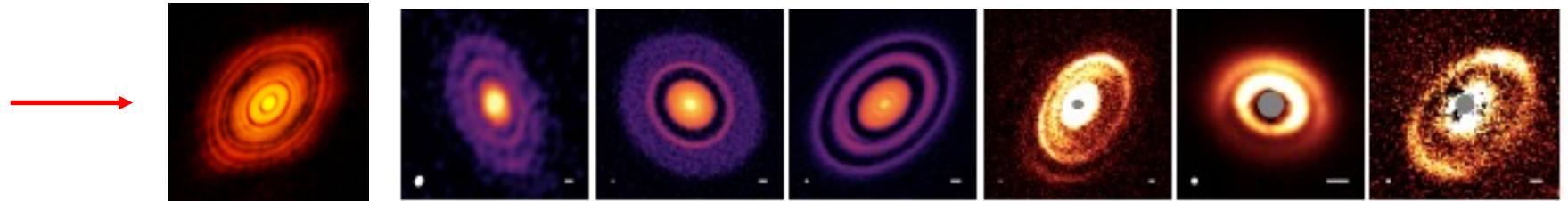
# *Protoplanetary discs observations*

Many observed bright targets are showing *substructures* in high resolution images of the dust continuum and in scattered light:

ALMA partnership, Nov. 2014

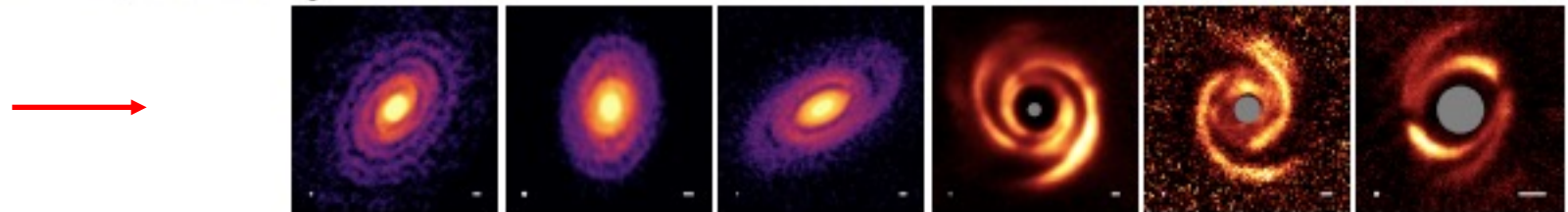
Rings

Gaps



Cavities

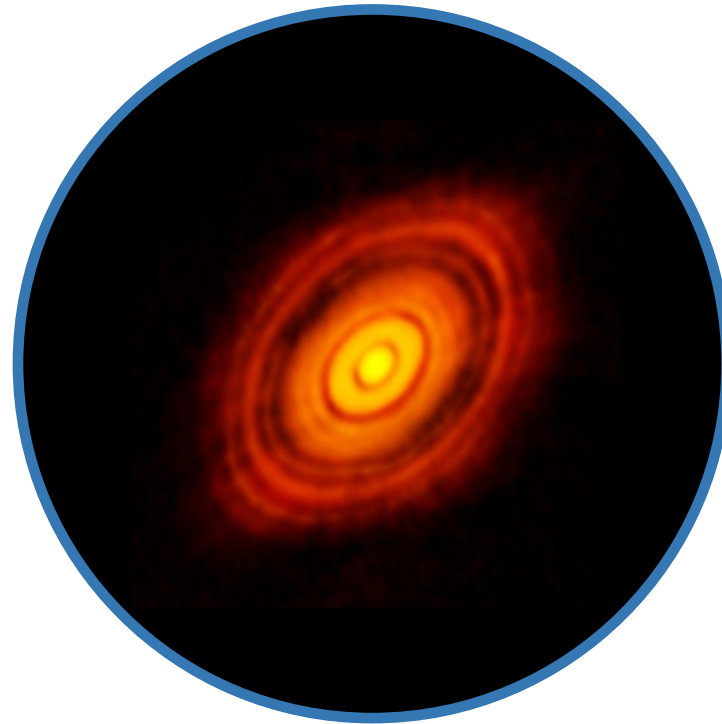
Spirals



# *Substructures*

ALMA partnership, Nov. 2014

Dust grains *trapped*  
in a pressure maxima  
(Pinilla et al. 2012, Dullemond et al.  
2018, Rosotti et al. 2020 +...)

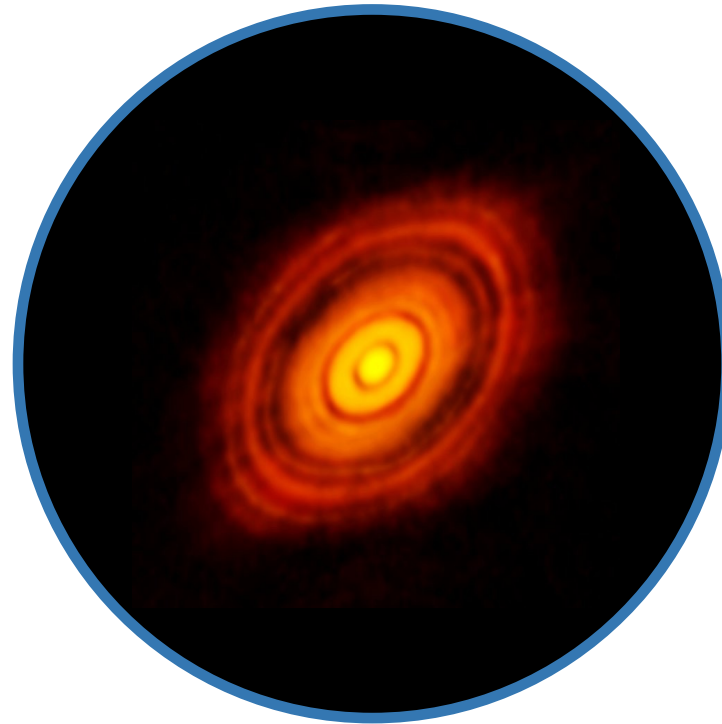


Induced *without* a  
pressure maxima, e.g.  
due to different opacity  
in different positions,  
snowlines  
(Stammler et al. 2017, ..)

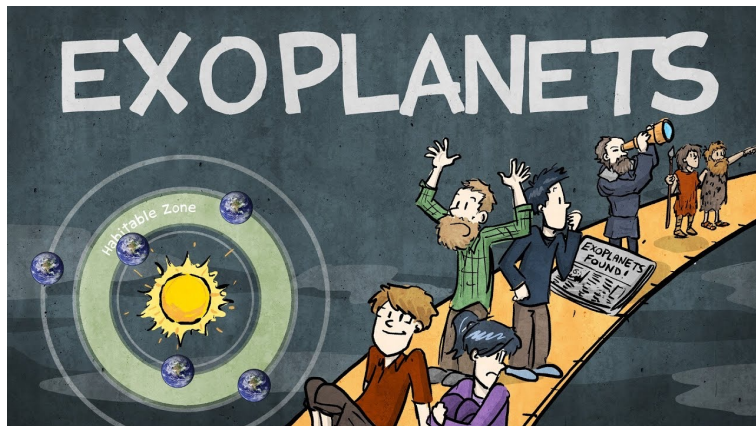
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From: PhDcomics.com

# *Not only bright discs...*

Try to study how fast an inhabitant of planet Earth runs the 100 m:

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Area	Men				Women			
	Time (s)	Wind (m/s)	Athlete	Nation	Time (s)	Wind (m/s)	Athlete	Nation
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Europe ( <i>records</i> )	<b>9.80</b>	+0.1	Marcell Jacobs	Italy	<b>10.73</b>	+2.0	Christine Arron	France
North, Central America and Caribbean ( <i>records</i> )	<b>9.58 WR</b>	+0.9	Usain Bolt	Jamaica	<b>10.49 WR</b>	0.0 <sup>[a]</sup>	Florence Griffith-Joyner	United States
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Vs.

Average researcher (trained): 12-14 "

Average researcher (untrained): 15-20 "

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**Demographic studies!!!!**



# *A large amount of information*

Surveys of star forming regions investigate how disc properties vary with age and are a test-bed for disc evolution theories

## Lupus

Ansdell et al. 2016,2018  
Tazzari et al.  
2017,2020,2021  
Hendler et al. 2020,  
Sanchis et al. 2021  
Young  
1-3 Myr

## Taurus

Long et al. 2019  
Kurtovich et al. 2021  
Young  
1-2 Myr

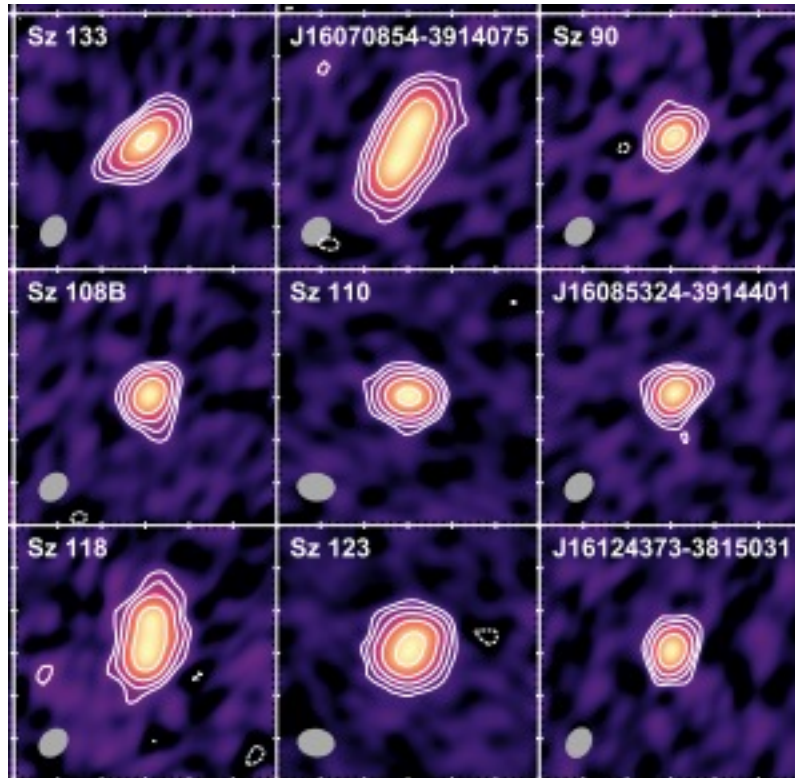
## Upper Sco

Barenfeld 2016,  
Hendler 2017  
Old  
5-10 Myr

- Lower resolution
- “High” statistics
- Masses
- Dust disc radii
- Gas disc radii

# *A large amount of information (II)*

Surveys of star forming regions investigate how disc properties vary with age and are a test-bed for disc evolution theories



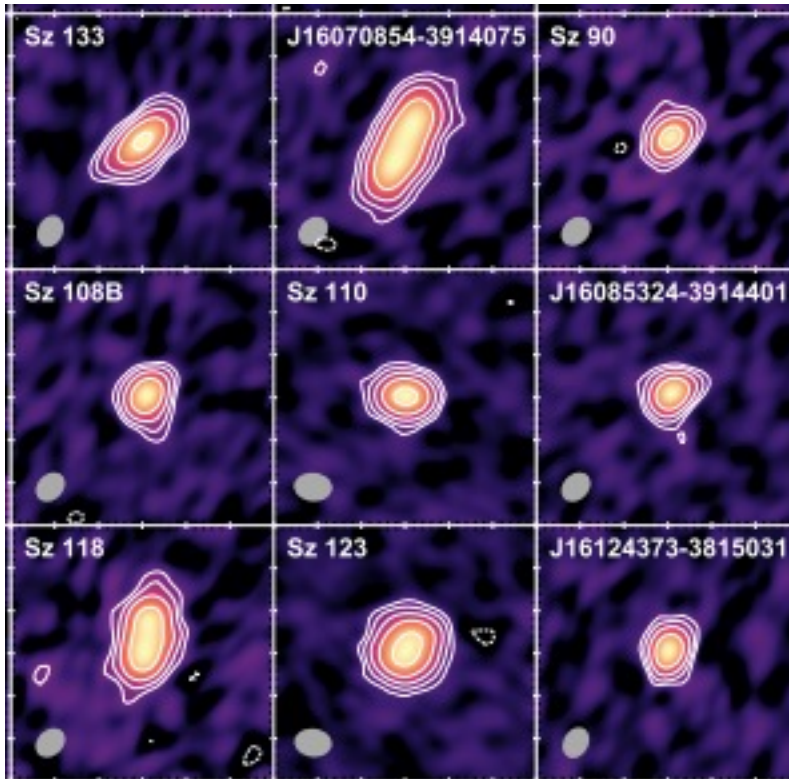
- dust disc radii 10 - 80 au

Unresolved  
substructures or  
smooth?

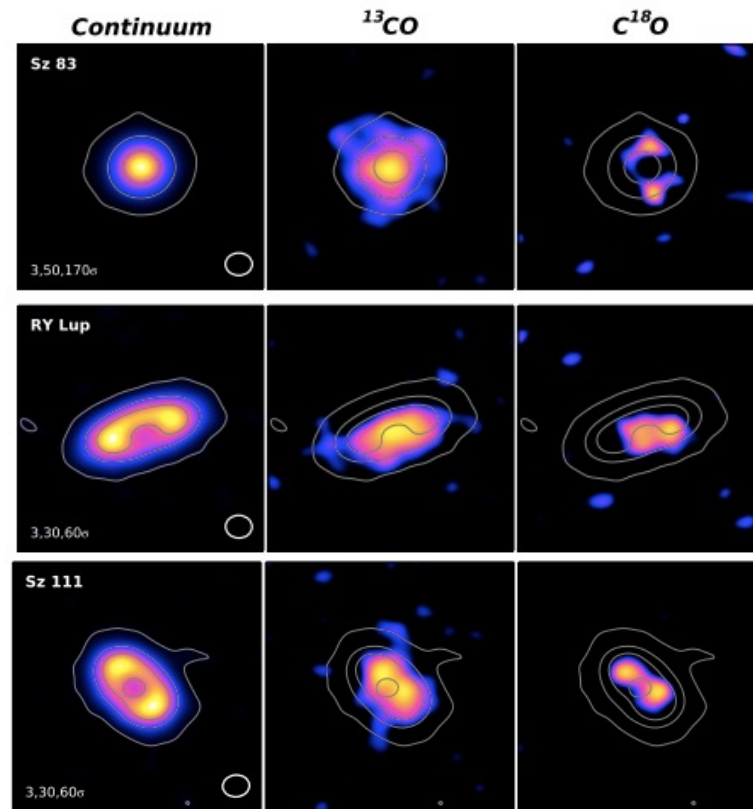
Tazzari et al. 2020, Lupus survey:  
continuum 3 mm (3"x3")

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Tazzari et al. 2020, Lupus survey:  
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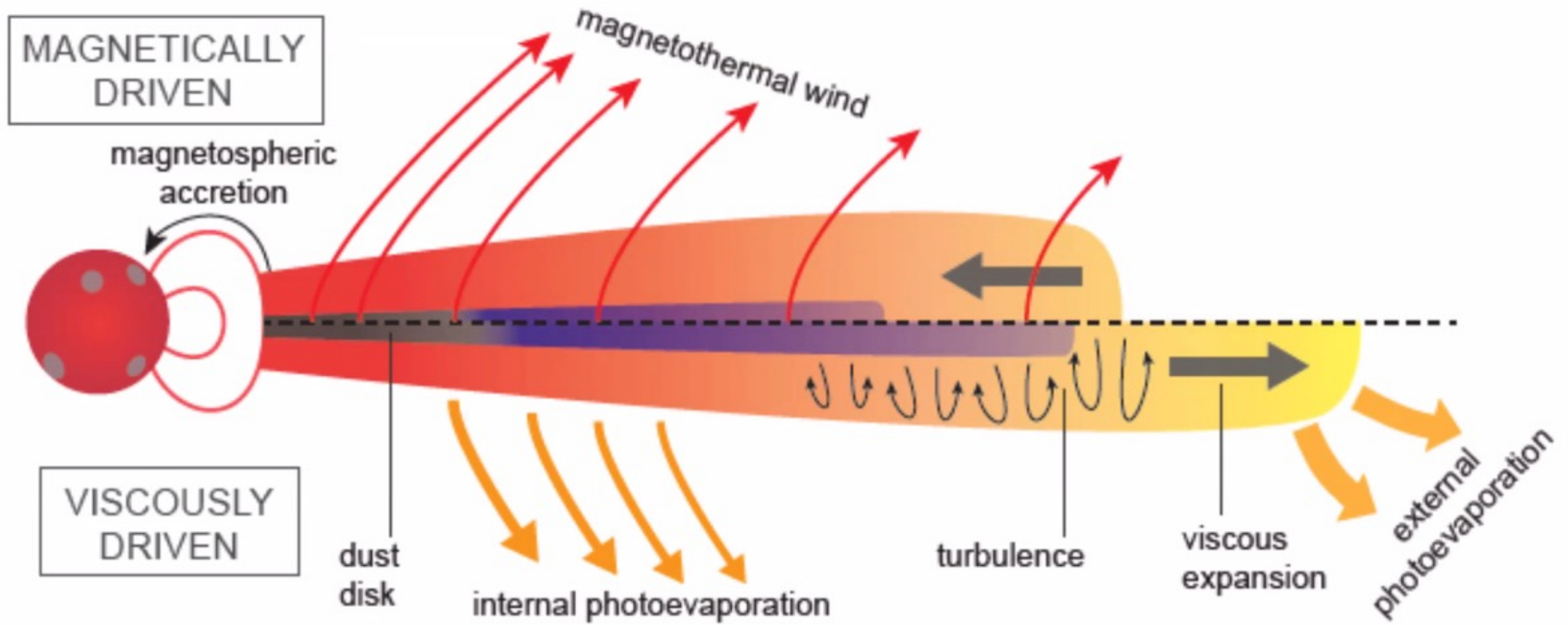


Ansdell et al. 2016, cycle 2 Lupus:  
CO isotopologues and 0,890 mm, (3"x3")

- dust disc radii 10 - 80 au
- Gas disc radii (more difficult, time consuming, missing data) 20-200 au

Unresolved  
substructures or  
smooth?

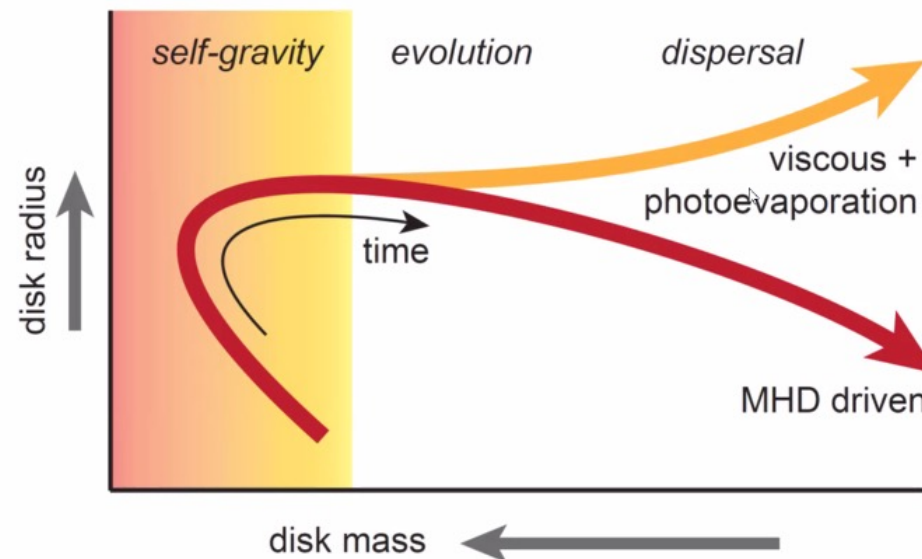
# The big debate



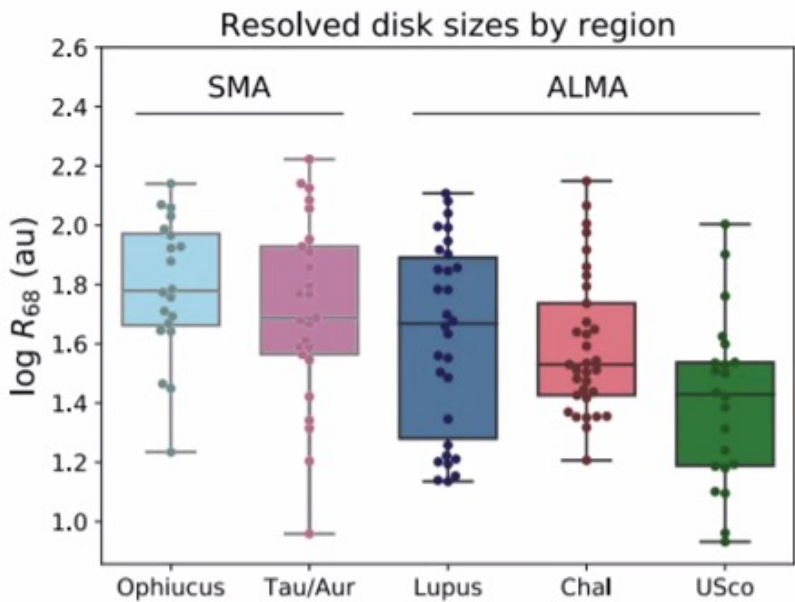
# *The global evolution of discs*

To understand which is the mechanism that is governing disc evolution we need to find a tracer that is sensitive to the global evolution of the disc.

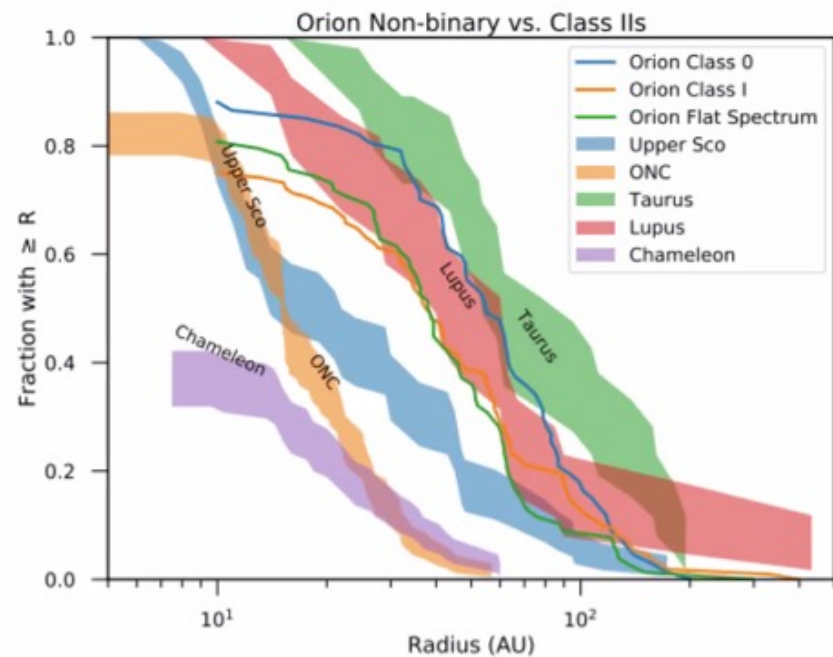
## Radius evolution



# Dust radii



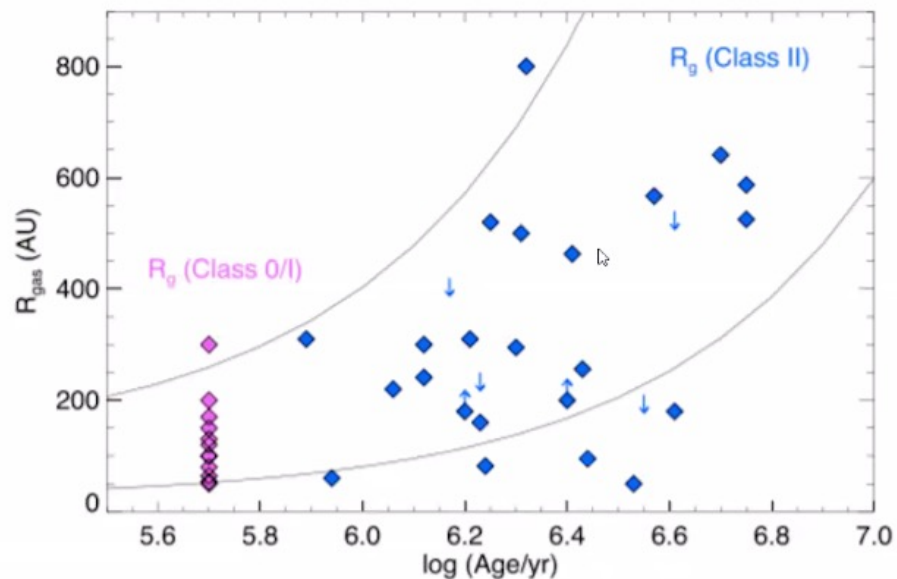
Hendler+ 2020



Tobin+ 2020

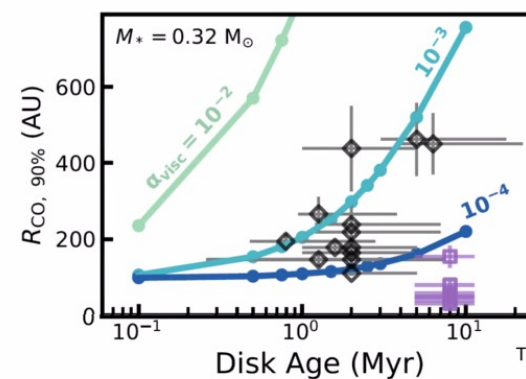
Class 0/I unclear but otherwise shrinking observed

# Evidence of viscous spreading?

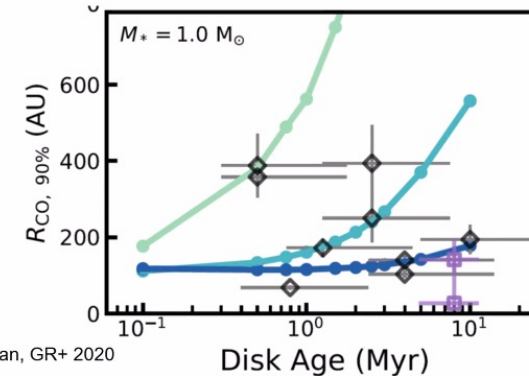


Najita & Bergin 2018

Tentative evidence, but inhomogeneous sample



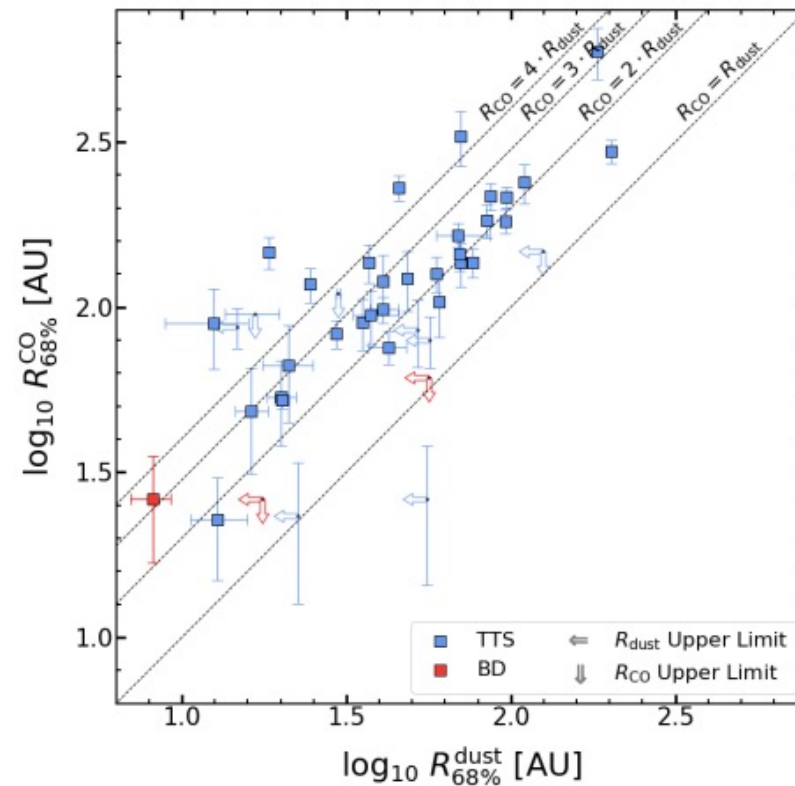
Trapman, GR+ 2020



Excludes discs are highly viscous: observed discs are not large enough  
Data too sparse to confirm/reject that disc size increases with time

# *A large amount of information (III)*

Surveys of star forming regions investigate how disc properties vary with age and are a test for disc evolution theories



- $R_{\text{CO}}/R_{\text{dust}}$  2-4 in Lupus

- 15% of the population  $R_{\text{CO}}/R_{\text{d}}$  > 4

Lupus population evolve similarly and is in the same evolutionary stage?

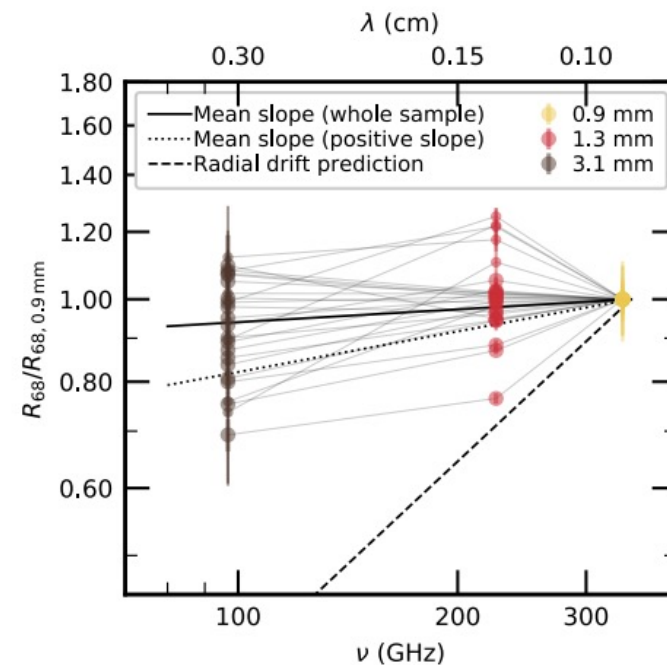


# What can we learn from dust radii?

$R_{\text{dust}}$

- The value of the radius depends on the dust opacity (large grains) (Rosotti et al. 2019)
- Lupus discs have nearly identical dust radius if observed at different wavelengths (Tazzari et al. 2021, see Marco's talk)
- Smooth and compact models reproduce observed dust flux- $M_{\text{dust}}$  relation. (Thripathi et al. 2018, Rosotti et al. 2019 a,b)
- Substructures can be common only in bright discs (Banzatti et al. 2020, van der Marel & Mulders 2021)

Lupus: Marco Tazzari's talk



- Nearly identical radii
- $R_{3\text{mm}}$  is  $\sim 90\%$   $R_{0.9\text{mm}}$

# *Disc evolution: dust*

Decoupled dust feels the gas like a headwind: lose energy and angular momentum

- Large grains drifts towards the star (Weidenschilling 1977)

## *Open question: understand the role of radial drift*

- Removes large grains
- Fast *shrinking* of the dust disc radii, eventually **disc disappearing** (timescale few  $10^5$  yr) (Appelgren et al. 2020)
- Substructures can slow down radial drift due to dust trapping (e.g., Pinilla et al. 2012), but are not observed in compact discs surveys (e.g., Sanchis et al. 2021)

# *Physical question: how much dust drifts in discs?*

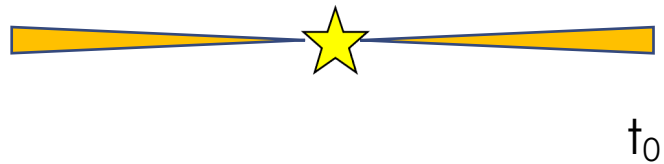
Do we really have a problem with radial drift?



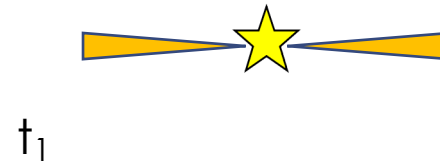
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Initial condition

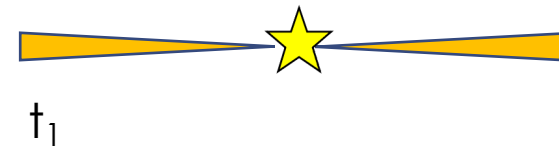
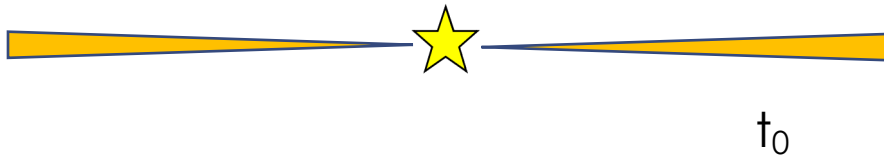


After a few Myr



compact disc

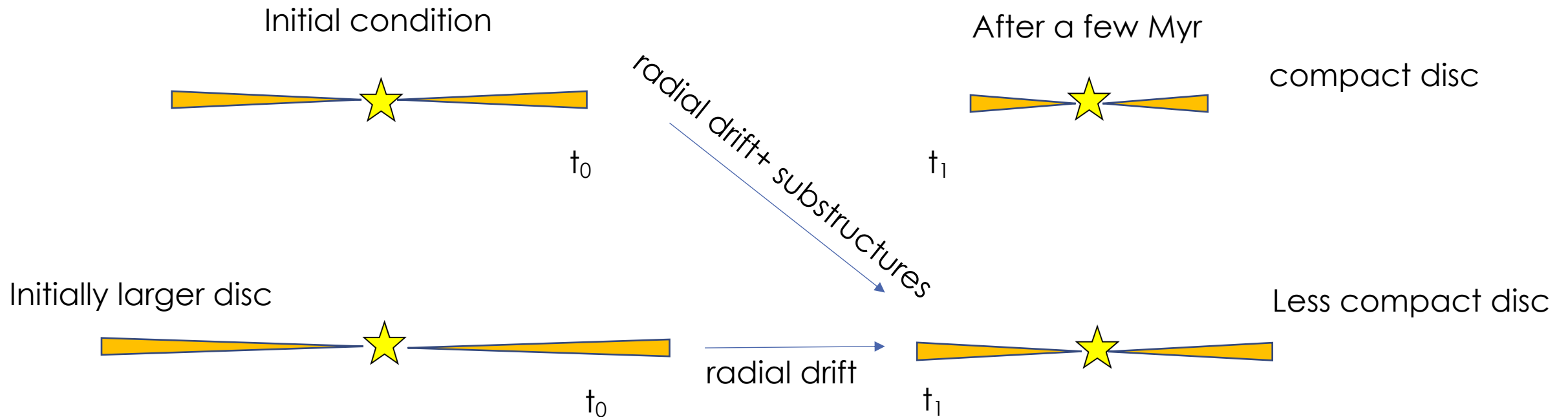
Initially larger disc



Less compact disc

# *Physical question: how much dust drifts in discs?*

Do we really have a problem with radial drift?



*Studying only dust radii we cannot solve this question*

# *What can we learn with gas radii?*

Gas dominates in mass. The physical process governing its evolution is linked to the mechanism driving the accretion on the star:

What do we observe?

Gas disc size as  
a function of the time  $R_{\text{CO}}$

Environmental evolution of CO  
Photodissociation, freeze-out,  
grain surface chemistry (see i.e.  
Trapman et al. 2020):

$R_{\text{CO}}$

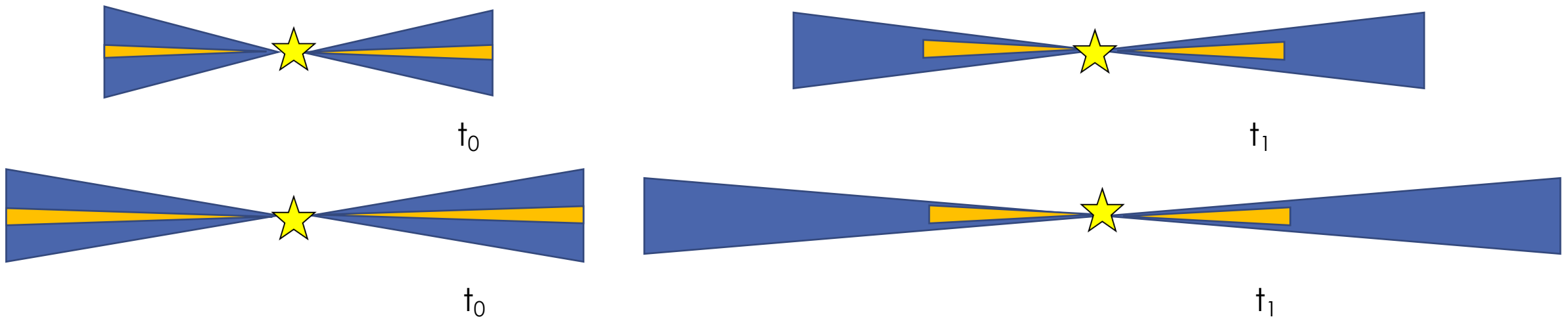
Gas radius (see i.e. Trapman et al. 2020):  
where CO is photodissociated

Viscous spreading

Not so easy to “measure” (see i.e.  
Trapman et al. 2020)

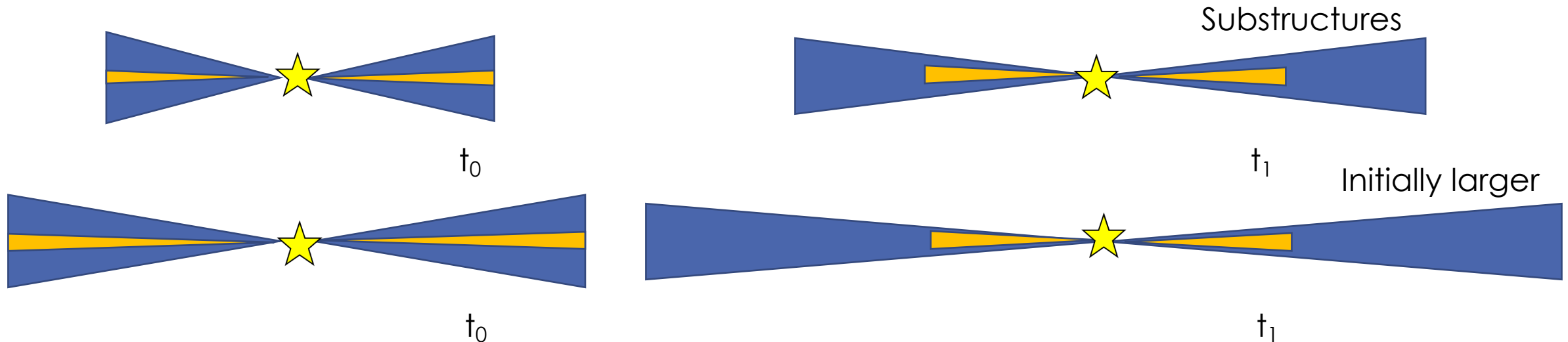
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- We can use the secular evolution of the ratio between the dust and gas radii,  $R_{\text{co}}/R_{\text{dust}}$ , capable to break the degeneracy



# *Physical question: how much dust drifts in discs?*

- We can use the secular evolution of the ratio between the dust and gas radii,  $R_{\text{co}}/R_{\text{dust}}$ , capable to break the degeneracy
- Follow up of Rosotti et al. 2019a,b (only dust sizes) testing how much dust drifts in synthetic population of discs with respect to the gas evolution





# *Our models*

1D synthetic discs composed by gas and dust

- Gas: viscous evolution
- 2 populations of dust (large and small grains) implemented as Birnstiel et al. 2012  
→ different dust to gas ratio each timestep (initially 100) **NEW!**
- Dust feedback considered (Laibe & Price 2014)
- Population evolved from 0-3 Myr
- Synthetic emission of CO lines  
with RADMC3D (Dullemond et al. 2012)
- Continuum 850 micron flux computed as in Rosotti et al. 2019 a,b  $S_b(R) = B_\nu(T(R))[1 - \exp(-\kappa_\nu \Sigma_d)]$

$R_{CO}$

Gas radius: 68% of the flux

$R_{dust}$

Dust radius: 68% of the flux

$B_\nu$  planck function  
 $\kappa_\nu$  opacity

# *Initial conditions*

Suite of models to probe the parameter space (No montecarlo), fixed stellar mass 1 Msun

Initial scale radius  $R_c$

**$R_c = 10, 30, 80$  au**

Poor constrained  
Recent surveys:  
discs initially compact  
Maury et al. 2019  
Tobin et al. 2020

Initial disc mass  $M_0$

**$M_0 = 0.01, 0.03, 0.1$  Msun**

Determines CO self-shielding  
Trapman et al. 2019  
Difficult to measure  
Miotello et al. 2017

Viscosity  $\alpha$

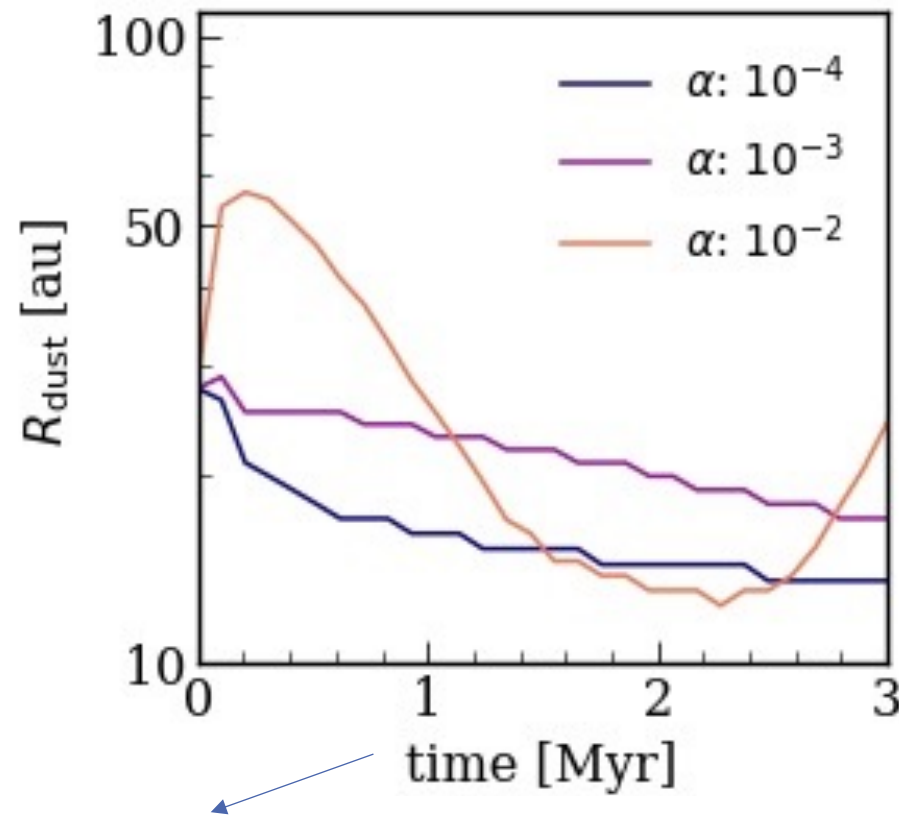
**$\alpha = 10^{-4}, 10^{-3}, 10^{-2}$**

Controls mass accretion rates  
and viscous spreading  
Trapman et al. 2020,  
Flaherty et al. 2017, 2020

Coming soon: Initial conditions for populations of discs (Somigliana + 2021)

# *This work $R_{\text{dust}}$*

Reference case:  $M_0=0.1 \text{ Msun}$ ,  $R_c=10 \text{ au}$



## Dust radius $R_{\text{dust}}$

$\alpha = \mathbf{10^{-4}, 10^{-3}}$

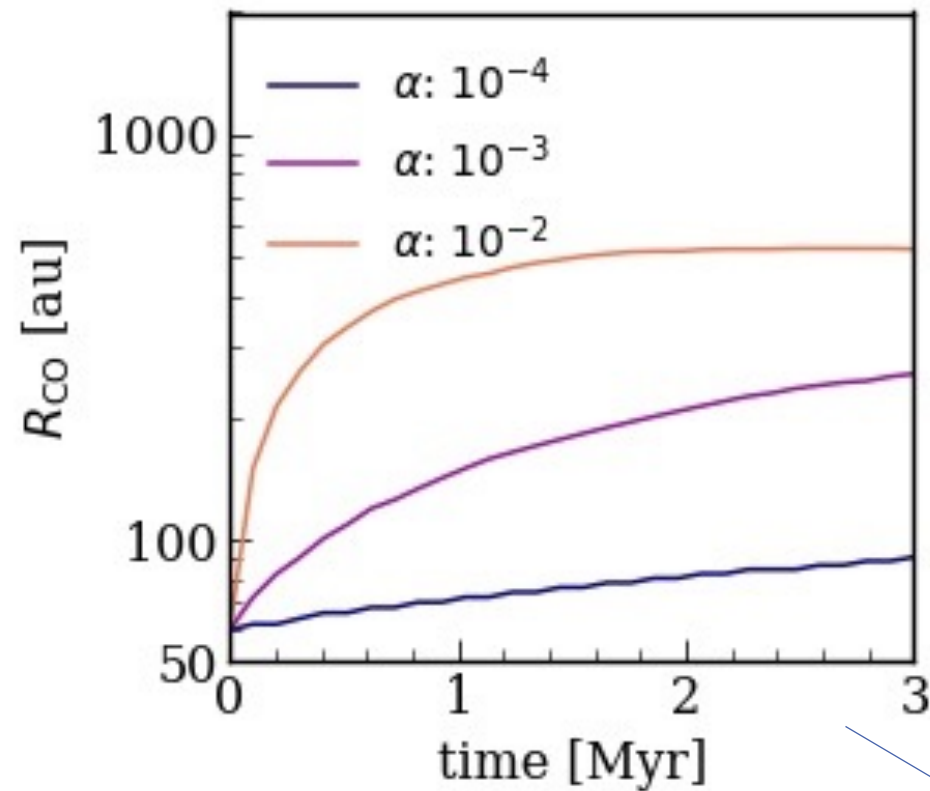
- Dust radii decreases with time: radial drift is at play: dust radii becomes 20 -10 au after 1 Myr

$\alpha = \mathbf{10^{-2}}$

- Two phases of expansion: due to viscous spreading (grains still grow) and due to the opacity cliff

# *This work $R_{CO}$*

Reference case:  $M_0=0.1 \text{ Msun}$ ,  $R_C=10 \text{ au}$



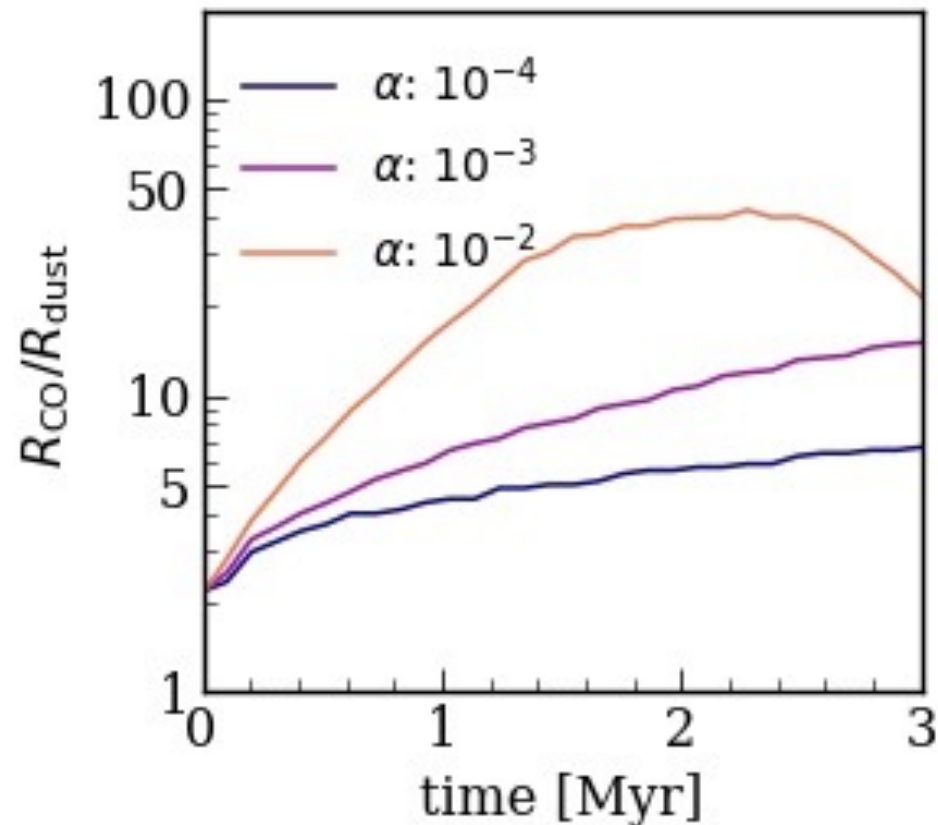
In agreement with  
Trapman et al. 2019,2020

## Gas radius $R_{CO}$

- viscous spreading at play, but not so easy to see after 1 Myr ...  
initial faster growing for larger values of  $\alpha$
- Very large values for high viscosity  $\alpha$
- Surface density decreases  $\rightarrow$   
enhancement of the CO photodissociation

# ***This work $R_{CO}/R_{dust}$***

Reference case:  $M_0=0.1 M_{sun}$ ,  $R_c=10$  au



## Ratio $R_{CO}/R_{dust}$

- Value of the viscosity crucial
- Starts with a relatively high value (2)

$\alpha = \mathbf{10^{-4}, 10^{-3}}$

- Monotonically increases to  $>4$

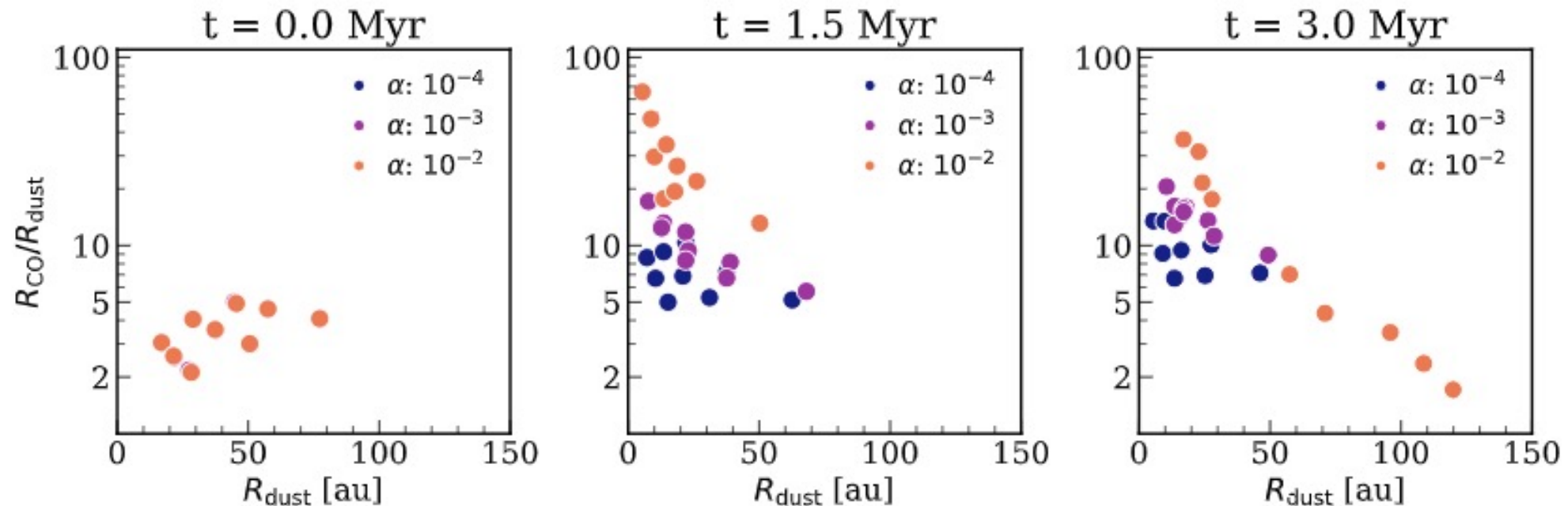
$\alpha = \mathbf{10^{-2}}$

- Grows to 50 then decreases to 20

... in any case *larger* than 4

# *Secular evolution*

How our models would appear if observed at a certain time?

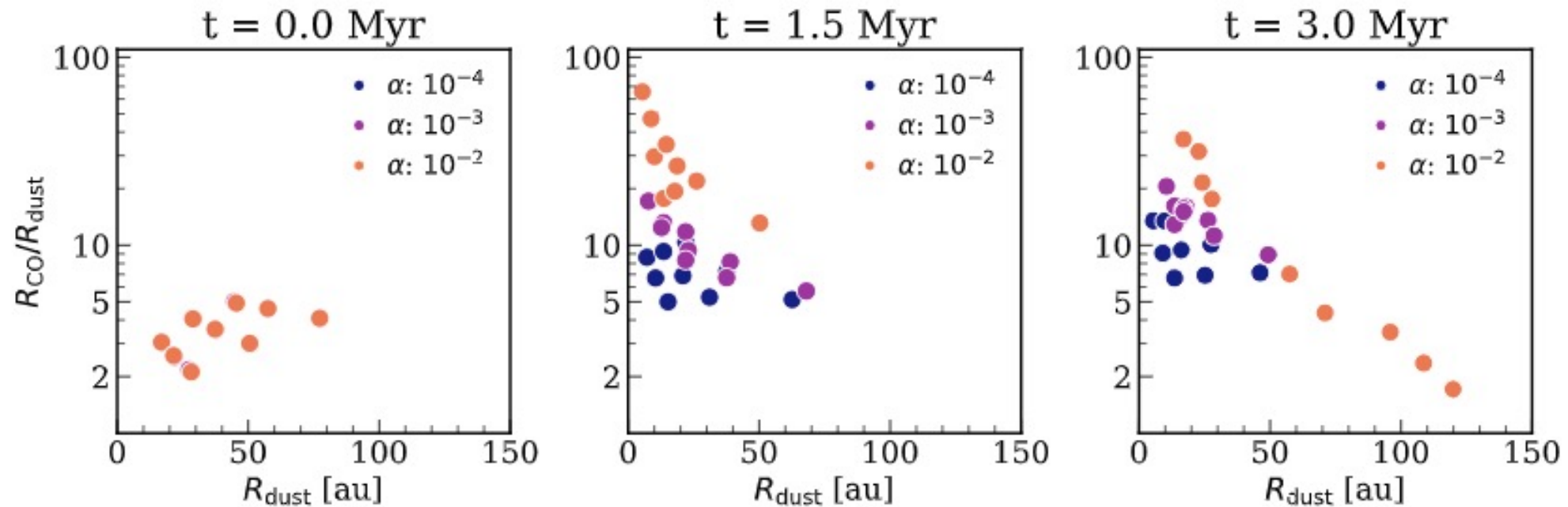


Linear span:  
no age spreading,  
no montecarlo

Note that we cannot cover the other parts of the plot  
(according to observations)

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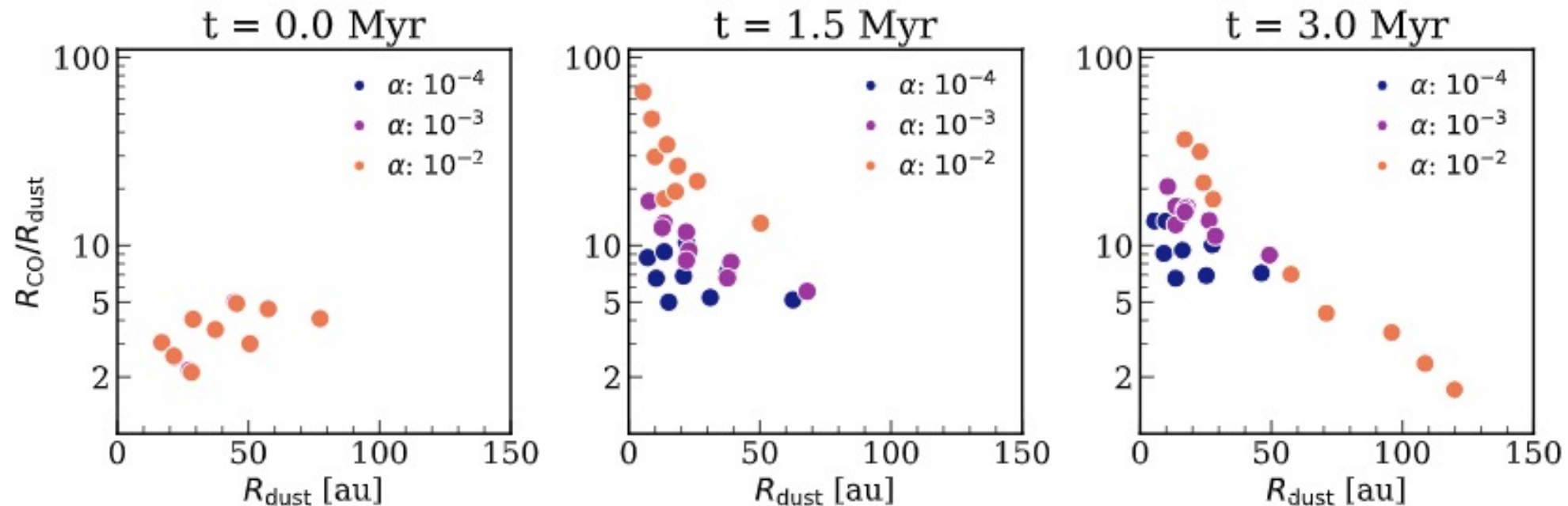


$R_{\text{dust}} < 60$

Very large gas radii for all the values of the viscosity

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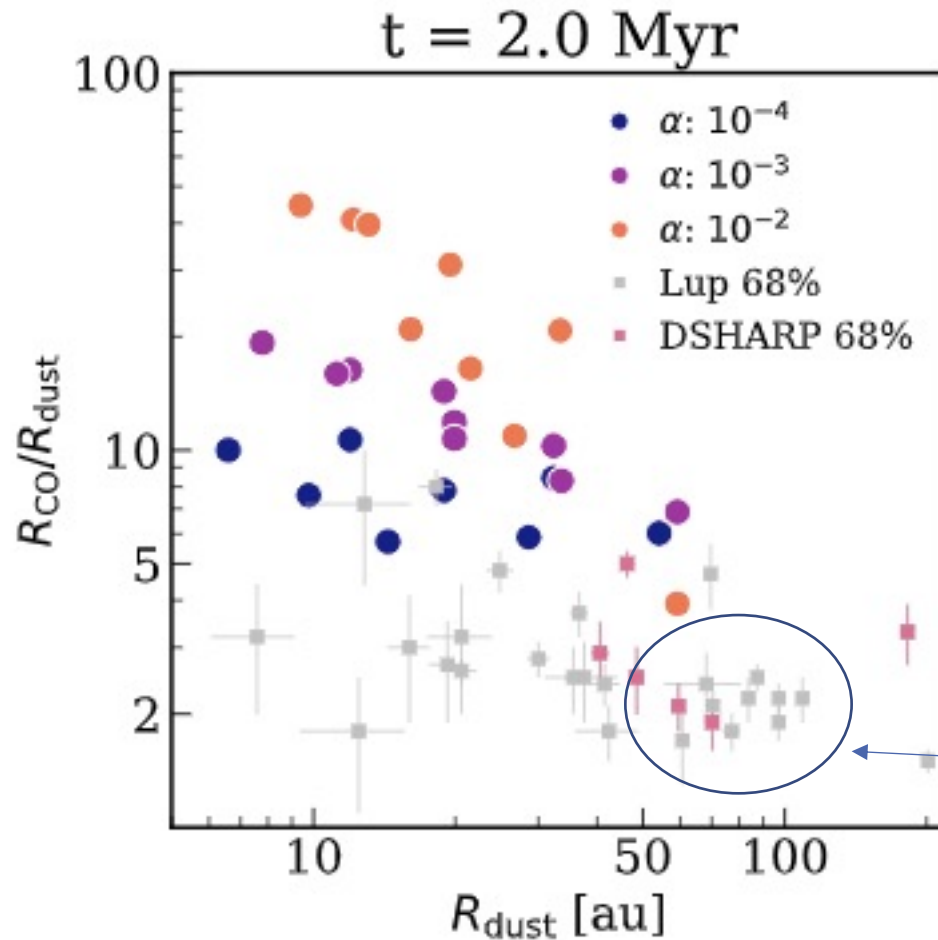
Very large gas radii for all small and intermediate values of the viscosity

$R_{\text{dust}} > 60$

Very large dust radii high value of viscosity (opacity cliff)



# Comparison with observations (*Lupus*)



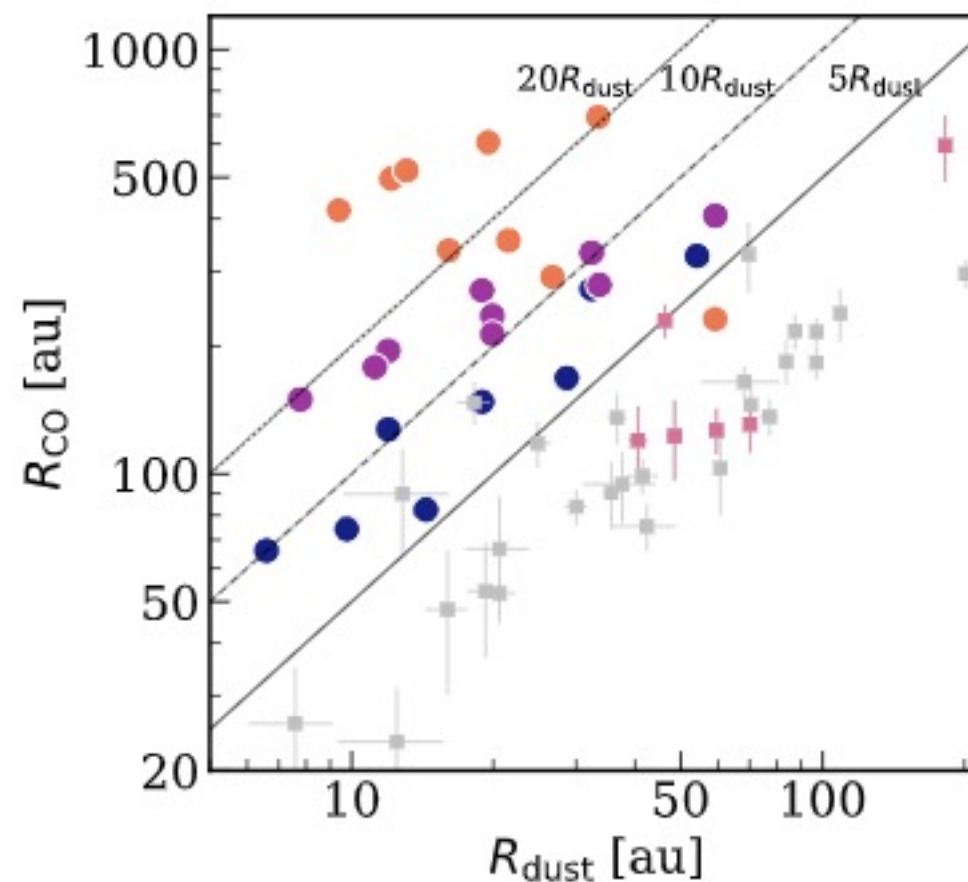
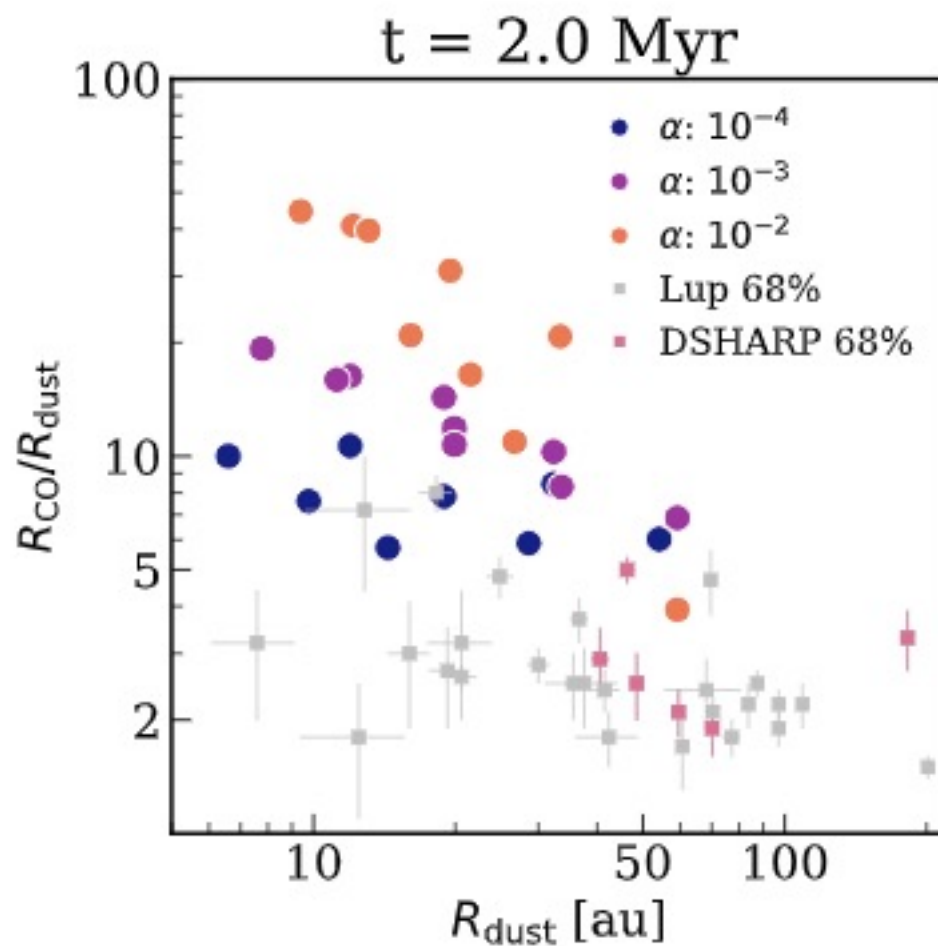
Our models do not reproduce the observed ratio of  $R_{\text{CO}} / R_{\text{dust}}$  in Lupus survey

- Too large ( $>2-3$  times)  $R_{\text{CO}} / R_{\text{dust}}$
- Dust disc radii  $R_{\text{dust}}$  too small

Discs with substructures

# Comparison with observations (*Lupus*)

Gas sizes almost ok, dust sizes too small!



# ***Possible solutions: slower growth?***

1)  $R_{\text{dust}}$  is too small: less efficient radial drift?

Explore different dust growth timescale in the 2 population model of Birnstiel et al. 2012, as Booth & Owen 2020 and Sellek et al. 2020:

$$t_g = \frac{a}{\dot{a}} = f_{\text{grow}} \left( \frac{\Sigma_g}{\Sigma_d \Omega} \right)$$

$f_{\text{grow}}=1 \rightarrow$  all the collision results in growth  
 $f_{\text{grow}}=100 \rightarrow$  1% of the collision results in growth

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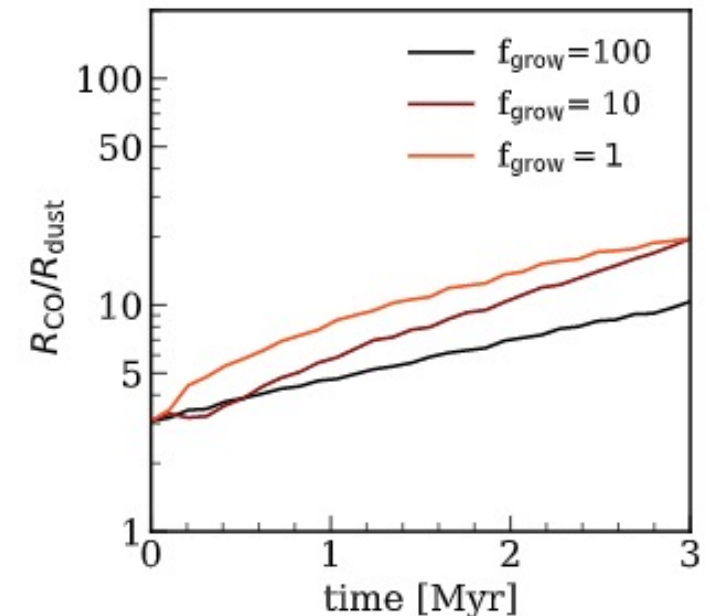
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Needs  $f_{\text{grow}}=100$  (= block dust evolution)  
 $\rightarrow$  very strong dependence on the initial conditions

Leads to a final disc mass  $f_{\text{grow}}$  times larger, problems to explain Upper Sco masses (Sellek et al. 2020)



# *Possible solutions: MHD winds?*

## 2) $R_{\text{CO}}$ is too large: MHD winds?

If angular momentum of gas is removed due to disc—wind interactions discs sizes should not grow with time (Suzuki 2016, Bai 2016)



- Reduce the values of  $R_{\text{CO}} / R_{\text{dust}}$



- Strong constraint on the efficiency of disc winds  
(needs to remove a large fraction of the disc mass)



- Not solving the  $R_{\text{dust}}$  problem: still needs a way to slow down radial drift

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- Not solving the  $R_{\text{dust}}$  problem: still needs a way to slow down radial drift



Future work is coming (Alice's Ph.D. project, B. Tabone's paper, ..)

# *Possible solutions: Different chemical evolution?*

## 3) $R_{\text{CO}}$ is too large: Different CO abundances?

10 -100 times lower abundance of CO found by several authors  
(Favre et al. 2013) (Turbulent mixing)



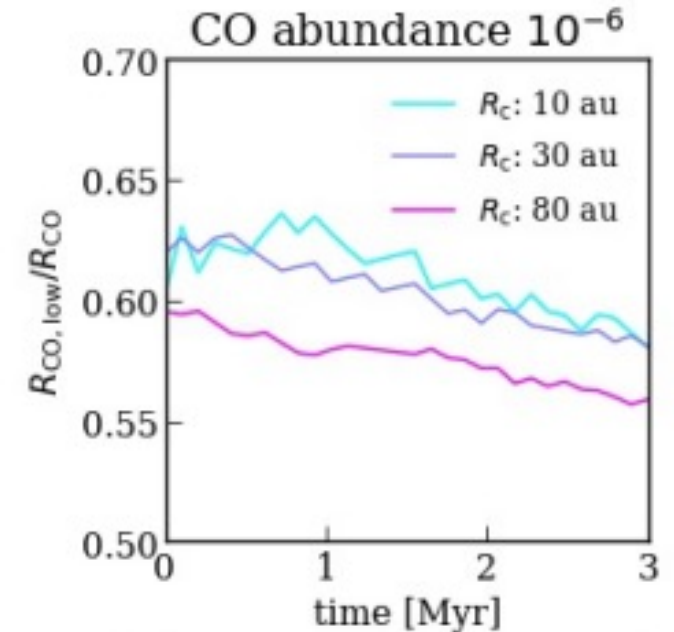
- Abundances of  $10^{-6}$  reduce the values of  $R_{\text{CO}} / R_{\text{dust}}$



- Allows initially larger discs  $R_{\text{c}}=30-50$  au

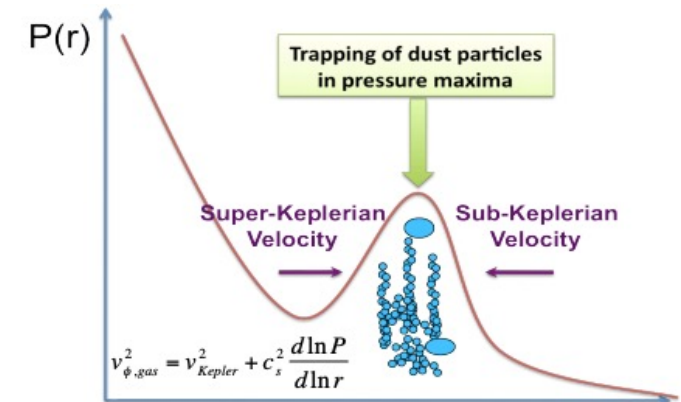


- Not solving the  $R_{\text{dust}}$  problem: still needs a way to slow down radial drift (less stringent)



# Possible solutions: Substructures!

4) Dust traps collecting the dust at pressure maxima  
(Whipple 1972, Pinilla et al. 2012, + ...)



e.g. Klahr & Henning (1997) ; Fromang & Nelson (2005); Johansen et al. (2009); Pinilla et al. (2012a)



- Increase the values of  $R_{\text{dust}}$  without changing  $R_{\text{CO}}$



- Reduce the values of  $R_{\text{CO}} / R_{\text{dust}}$



- No requirements for initial conditions or disc evolution

*Unresolved* substructures can be at play also in compact and faint discs, undetected

- All the mechanisms that creates substructures where dust is trapped can be at play! (e.g., Planets Lin & Papaloizou 1979 ..)



# *Possible solutions: Substructures!*

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Future work is coming (A. Zormpas paper, ...)

*Unresolved* substructures can be at play also in compact and faint discs, undetected

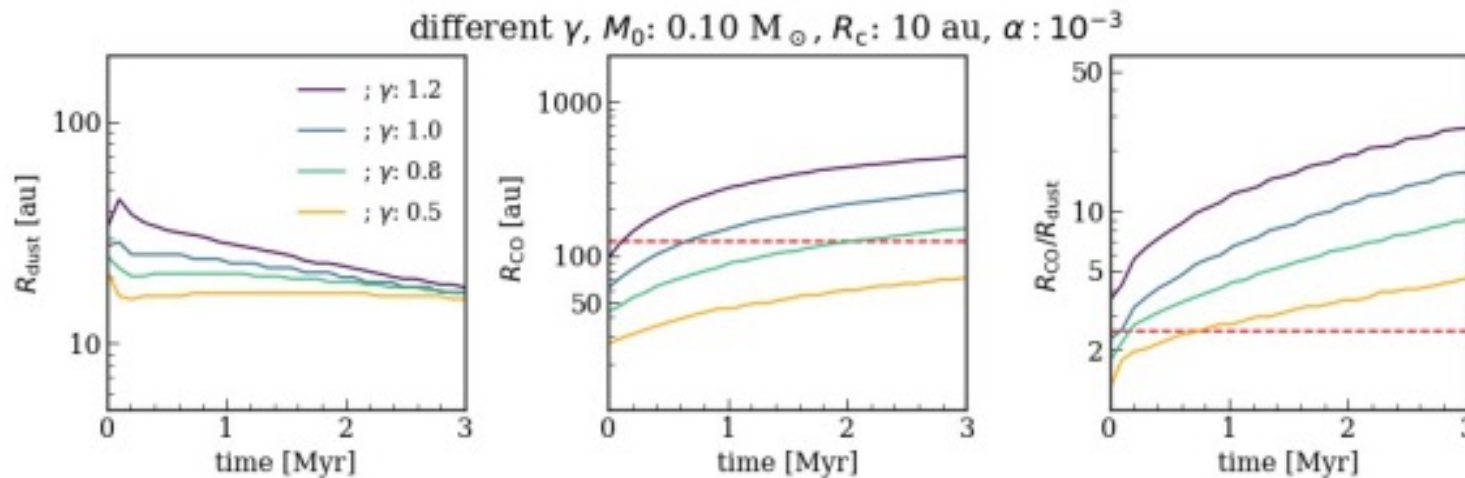
- *All* the mechanisms that creates substructures where dust is trapped can be at play! (e.g., Planets Lin & Papaloizou 1979 ..)

# Possible solutions: Different viscosity law?

5)  $R_{\text{CO}}$  is too large: effect of the shape of the surface density in the outer part of the disc?

Affects both the dust and gas sizes  $\rightarrow$  it is difficult to probe the outer part of discs

$$v = v_c(R/R_c)^\gamma$$

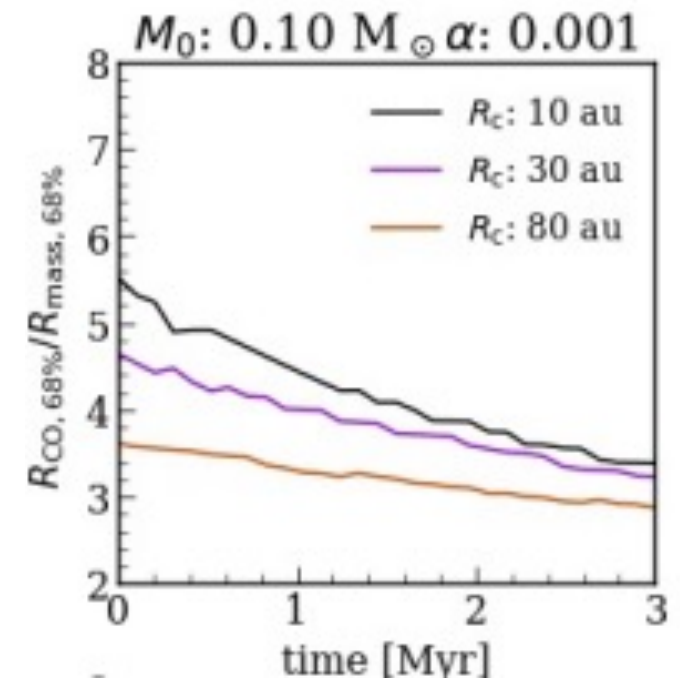


- Not solving the  $R_{\text{dust}}$  problem: still needs a way to slow down radial drift (less stringent)

# *Can we trust CO?*

$R_{\text{CO}}$  depends on the mass distribution in the outer part in the disc

- Not a good tracer for mass
- Not a good tracer for viscous spreading
- Not a good tracer for the scale radius of the disc



→ Explore other tracers as  $^{13}\text{CO}$  (but we need to improve our knowledge of the thermochemistry of discs)

# *Conclusions*

We modelled the secular evolution of  $R_{\text{CO}} / R_{\text{dust}}$  to test the efficiency of radial drift

- First models with dust growth + gas evolution
- Our results for dust and gas are in agreement with previous works (Rosotti et al. 2019, Trapman et al. 2019,2020)
- The values of  $R_{\text{dust}}$  are too small with respect to the observed values, leading to  $R_{\text{CO}} / R_{\text{dust}}$  values too large for all the values of the viscosity
- To solve this inconsistency unresolved substructures should be present in almost all the discs



# *Future work*

- Proper population synthesis  
(coming soon.... Somigliana et al. 2021)
- Analytical prescriptions for the gas size (Toci+ in prep,  
Trapman+ in prep)
- Environmental effects
- Different tracers
- Add substructures



*Thank you!*

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